



Boğaziçi University

**Introductory
Phys Labs**

1863

STEFAN- BOLTZMANN RADIATION LAW

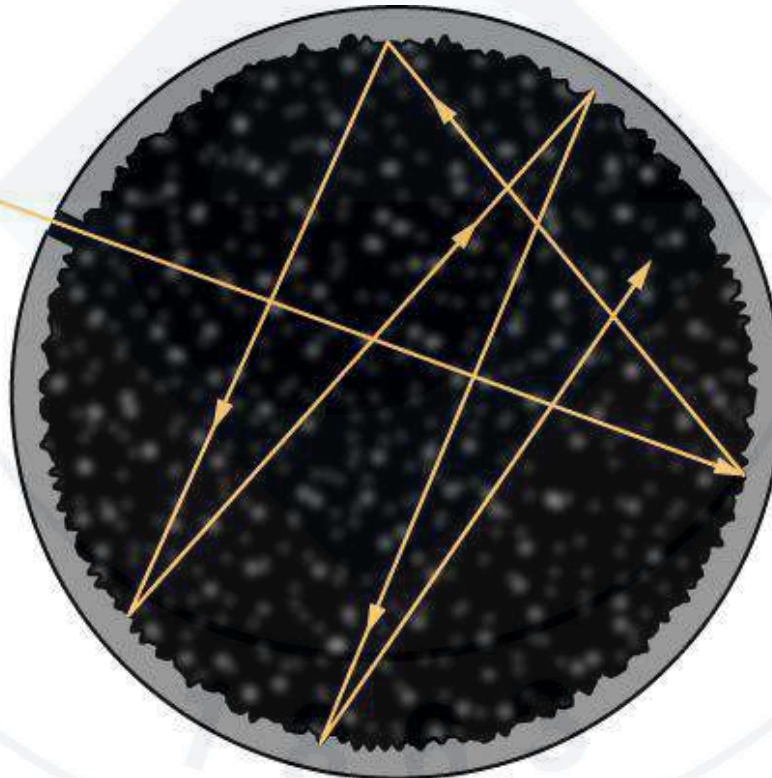
PHYL 202



THEORY

STEFAN-BOLTZMANN RADIATION LAW

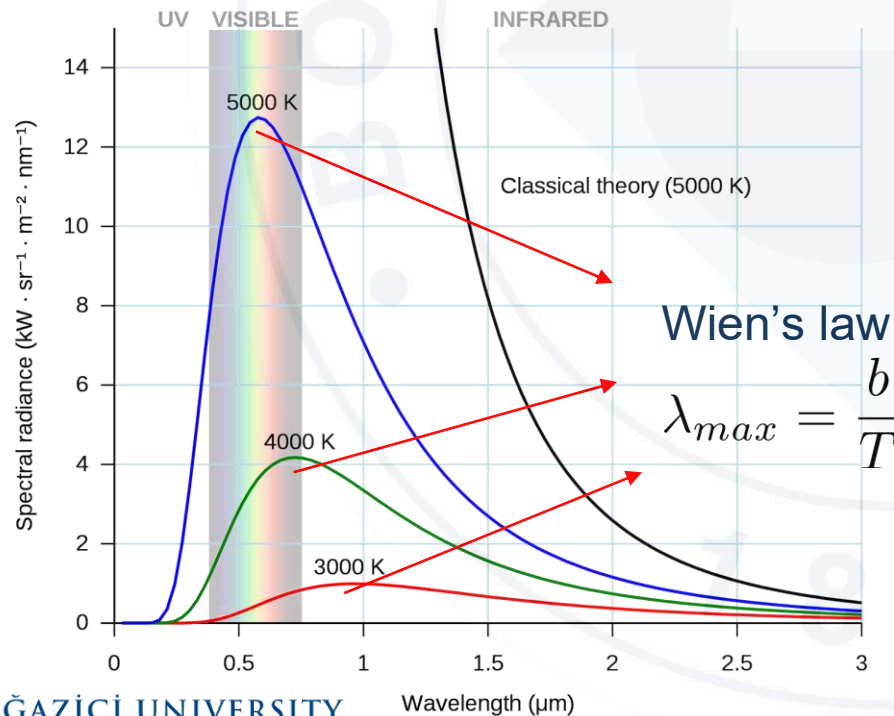
Definition of a black body: An idealized physical body that absorbs all incident electromagnetic radiation, regardless of frequency or angle of incidence



STEFAN-BOLTZMANN RADIATION LAW

Classical theory formed by Rayleigh and Jeans predicted at shorter wavelengths energy emitted by black-body tends to go infinity, hence the **ultraviolet catastrophe** and it is contradicted with experimental data.

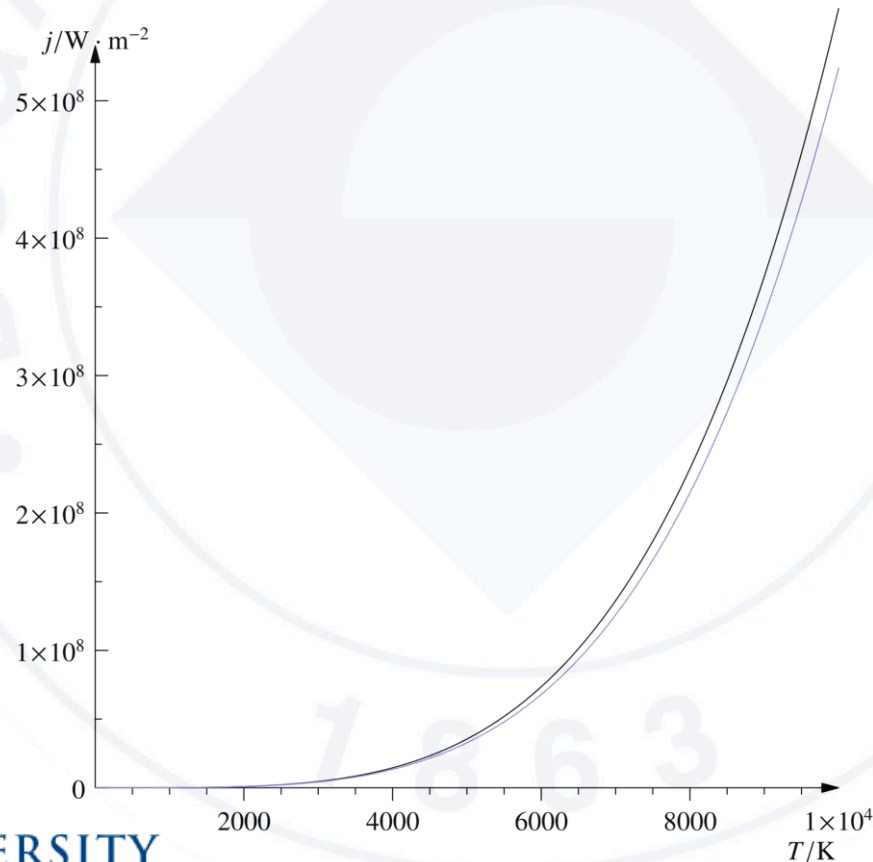
Planck transformed this idea by **quantizing** the energy inside of the cavity.



STEFAN-BOLTZMANN RADIATION LAW

Stefan-Boltzmann Law states that the total energy radiated per unit surface area of a black body at all wavelengths per unit time depends only on the temperature of the object

$$R = \sigma T^4$$



STEFAN-BOLTZMANN RADIATION LAW

- The proportionality constant is called as Stefan-Boltzmann constant and it is derived from other physical constants:

$$\sigma = \frac{2\pi^5 k_B^4}{15c^2 h^3} = 5.670373 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$$

where:

- k_B is Boltzmann constant
- h is Planck constant
- c is the speed of light.

If an object is not blackbody (it doesn't absorb all the incoming radiation at all wavelengths), the emitted energy is less than of black-body

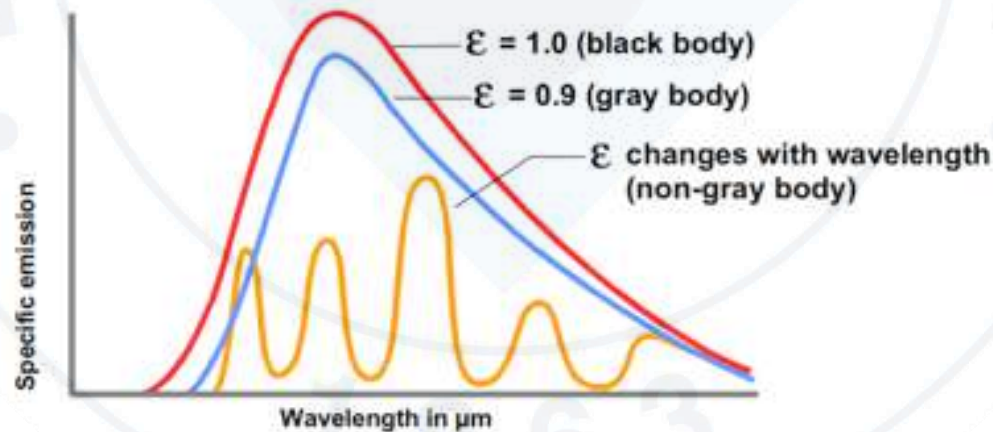
$$R = \epsilon \sigma T^4$$

where $\epsilon < 1$.

If an object is not blackbody (it doesn't absorb all the incoming radiation at all wavelengths), the emitted energy is less than of black-body

$$R = \epsilon \sigma T^4$$

where $\epsilon < 1$.

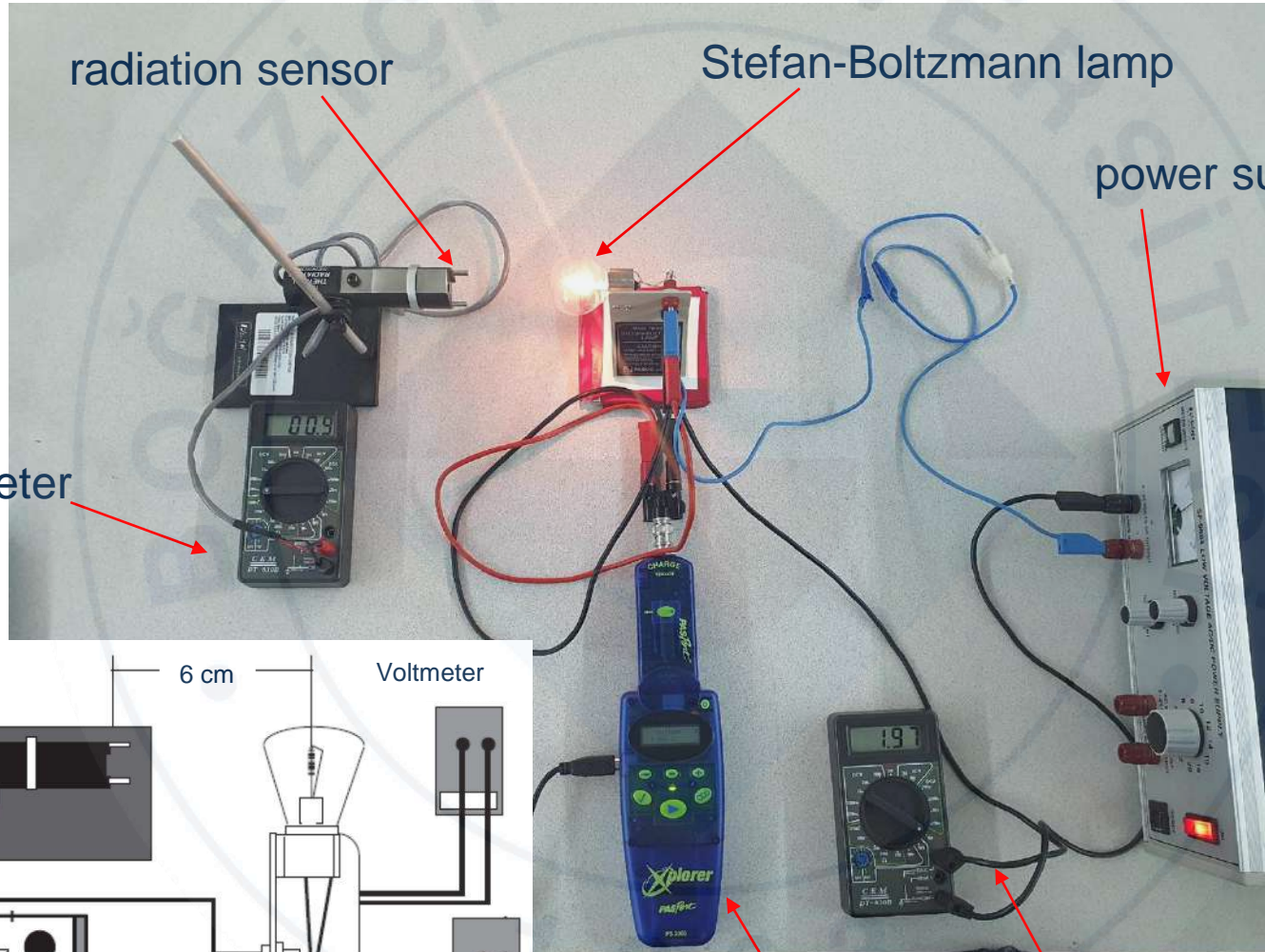


BOĞAZIÇI ÜNİVERSİTESİ

APPARATUS

1863

STEFAN-BOLTZMANN RADIATION LAW

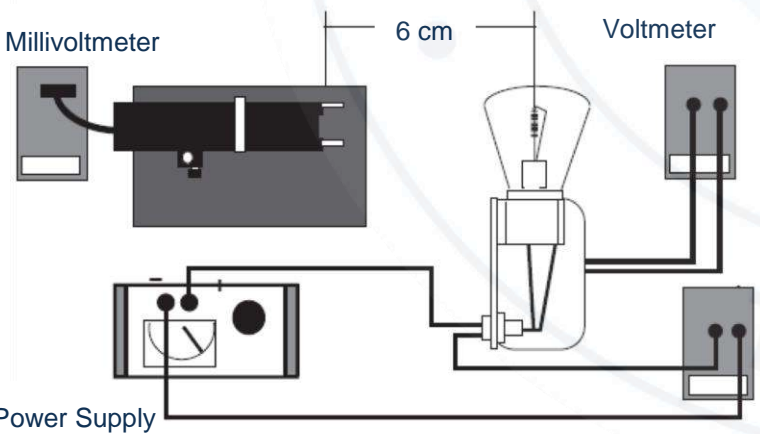


radiation sensor

Stefan-Boltzmann lamp

power supply

voltmeter



voltmeter

ammeter



EXPERIMENT

1863

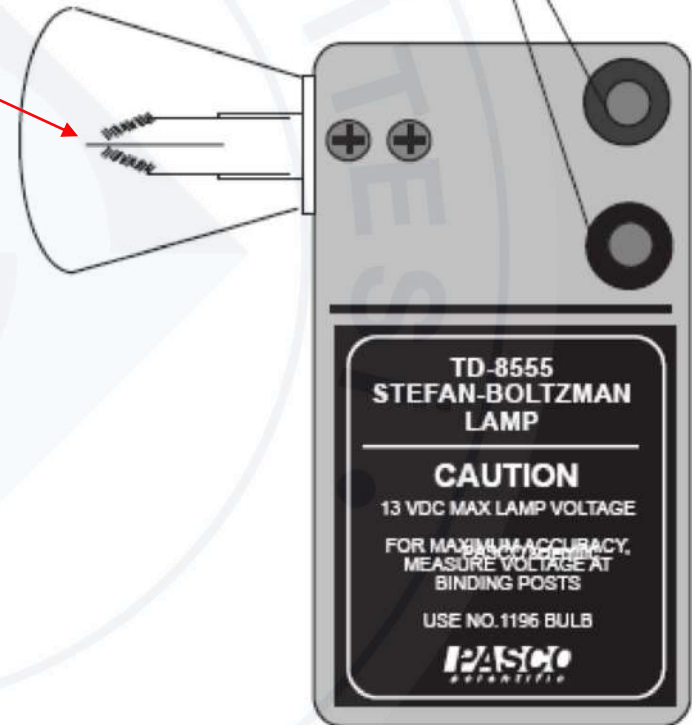
- The **objective** of our experiment is to determine rate of temperature dependency $R = \sigma T^n$ where $n_{TV} = 4$.
- In our experiment, the radiation sensor is only sensitive to infrared region of electromagnetic spectrum which turns Stefan-Boltzmann equation into a proportionality. $R \propto \epsilon\sigma T^4$

1863

STEFAN-BOLTZMANN RADIATION LAW

Measuring high temperatures inside a light bulb can be tricky! So instead of measuring a temperature of a **tungsten filament** of the lamp, we will measure voltage and corresponding current across the lamp at constant temperature, and calculate resistance by using Ohm's law.

Banana Connectors:
Connect to Power
Supply – 13 V MAX,
(2 A min, 3 A max)



1863

STEFAN-BOLTZMANN RADIATION LAW

From calculated resistance from the Ohm's law ($R=V/I$), we will calculate temperature with following formula

$$\frac{R}{R_0} = (1 + \alpha(T - T_0))$$

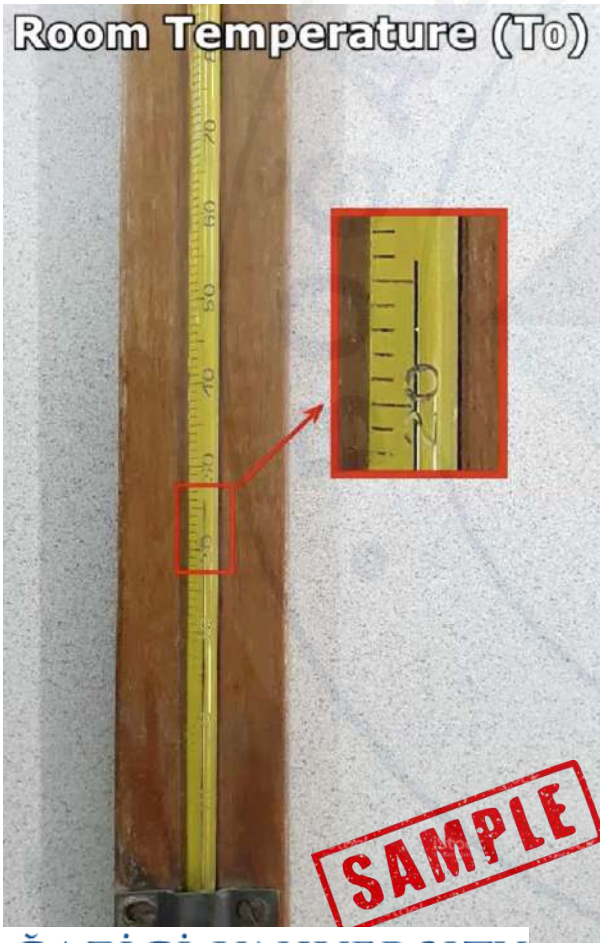
- R is the resistance at temperature T
- T_0 is the room temperature
- R_0 is the resistance of tungsten filament at room temperature
- α for tungsten is $4.5 \times 10^{-3} K^{-1}$

1863

STEFAN-BOLTZMANN RADIATION LAW

Measuring R_0 and T_0

- Set applied current to 0.20 A and measure V_0 and calculate R_0



radiation sensor
output in terms
of mV

voltage across
lamp (V)

current across
lamp (A)

STEFAN-BOLTZMANN RADIATION LAW

Draw the circuit diagram:

Write down the formula to calculate the temperature from the resistance

$$R/R_0 = (1 + \alpha(T - T_0)) \text{ Solve for T:}$$

$$\frac{R}{R_0} = (1 + \alpha(T - T_0))$$

T = **Solve for T**

$$T_0 = \text{Room temperature}$$

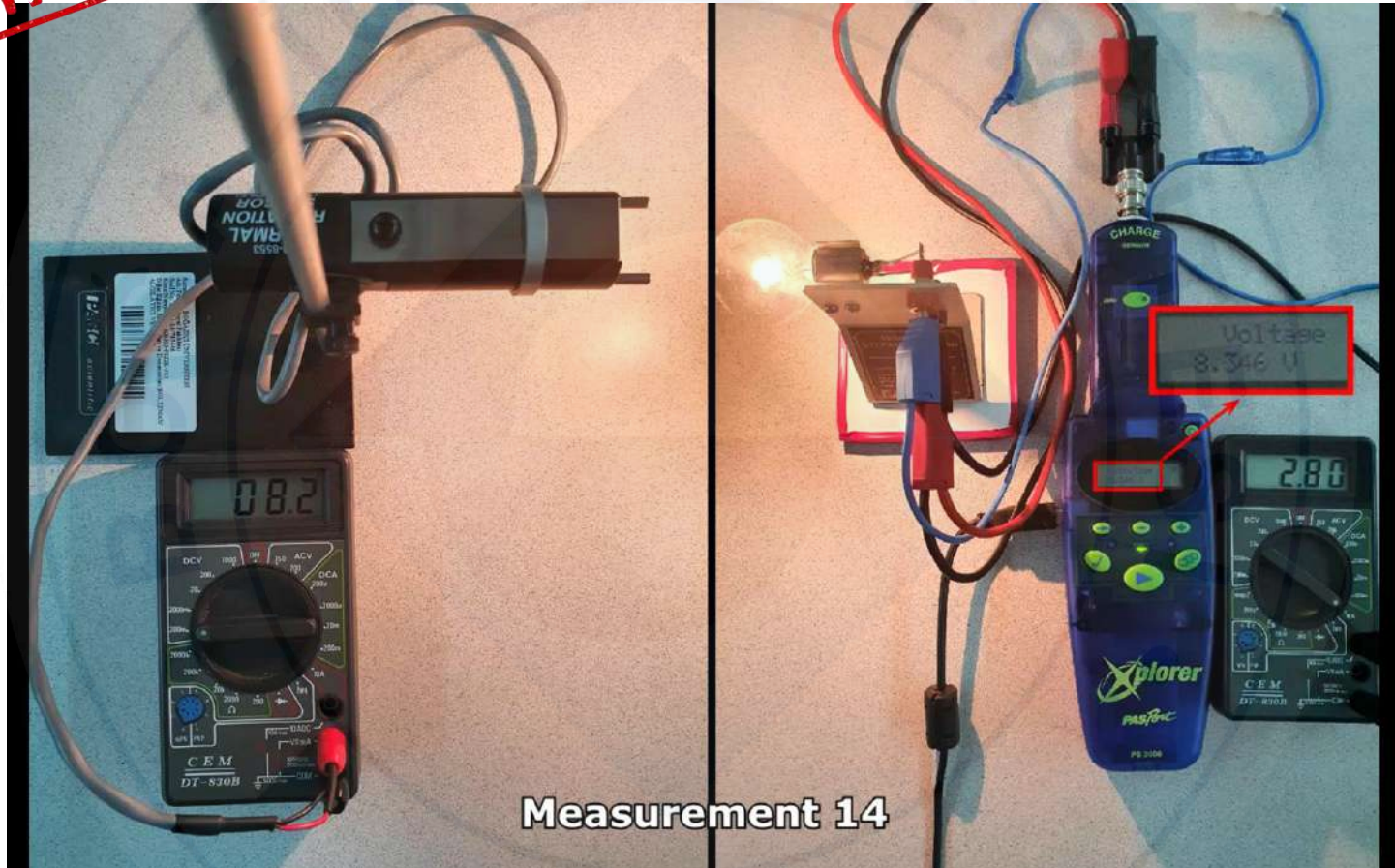
$$I_0 = 0.20 \text{ Amp.}$$

$$V_0 = \text{Measure!}$$

$$R_0 = \text{Calculate!}$$

$$\alpha = 4.403 \times 10^{-3} \text{ K}^{-1}$$

SAMPLE



Measurement 14

- Measure radiation sensor output, voltage & current across the lamp by the increment of 0.20 A.

STEFAN-BOLTZMANN RADIATION LAW

Ohm's Law

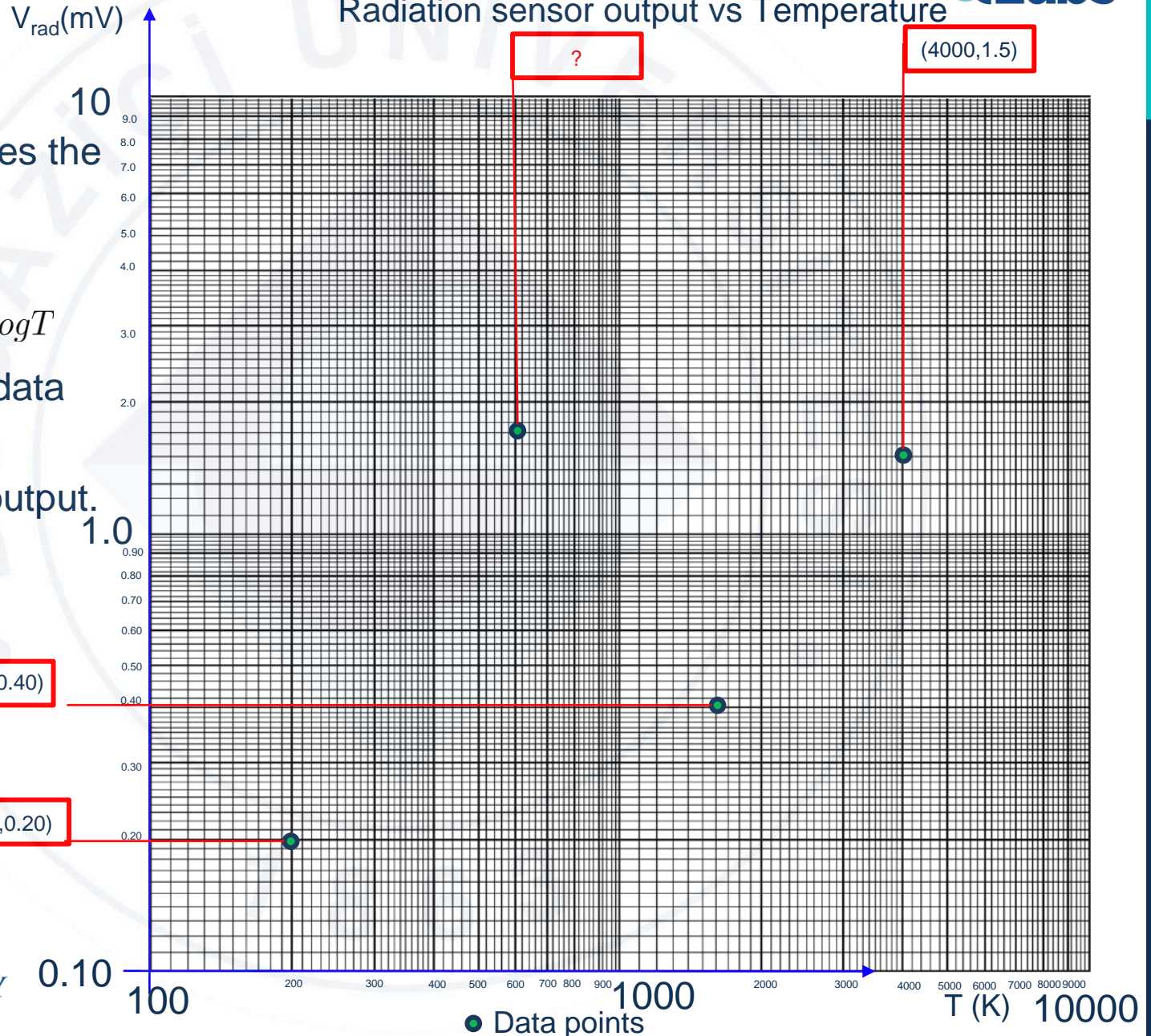


$$\frac{R}{R_0} = (1 + \alpha(T - T_0))$$

Current I ()	Potential Across the lamp V ()	Radiation Sensor output, V_{Rad} ()	Resistance of the filament, $R=V/I$ ()	R/R_0	Temperature of the filament, T ()

STEFAN-BOLTZMANN RADIATION LAW

Radiation sensor output vs Temperature



- Log-log graph takes the logarithm of the equation

$$\log R = \log \sigma + n \times \log T$$

- No need to draw data below 0.1 mV at radiation sensor output.

Don't forget to take the logarithm of the selected points!

$$\mathbf{n = SLOPE} = \dots m = \frac{\log y_2 - \log y_1}{\log x_2 - \log x_1} = \frac{\log\left(\frac{y_2}{y_1}\right)}{\log\left(\frac{x_2}{x_1}\right)} \dots$$

% error =

1863