



Boğaziçi University

# Introductory Phys Labs

# CHARACTERISTICS OF A CAPACITOR

**PHYL 201**

A large, faint, circular seal of Boğaziçi University is centered in the background. The seal contains the text "BOĞAZIÇI ÜNİVERSİTESİ" around the top and "1863" at the bottom. In the center of the seal is a diamond-shaped emblem with a sun-like symbol inside.

# THEORY AND APPARATUS

## CHARACTERISTICS OF A CAPACITOR

When you connect a capacitor and a resistor in series and apply a specific waveform, the behavior of the circuit can be understood by applying the Kirchoff's voltage law:

$$R \frac{dq}{dt} + \frac{q}{C} = V_{app}$$

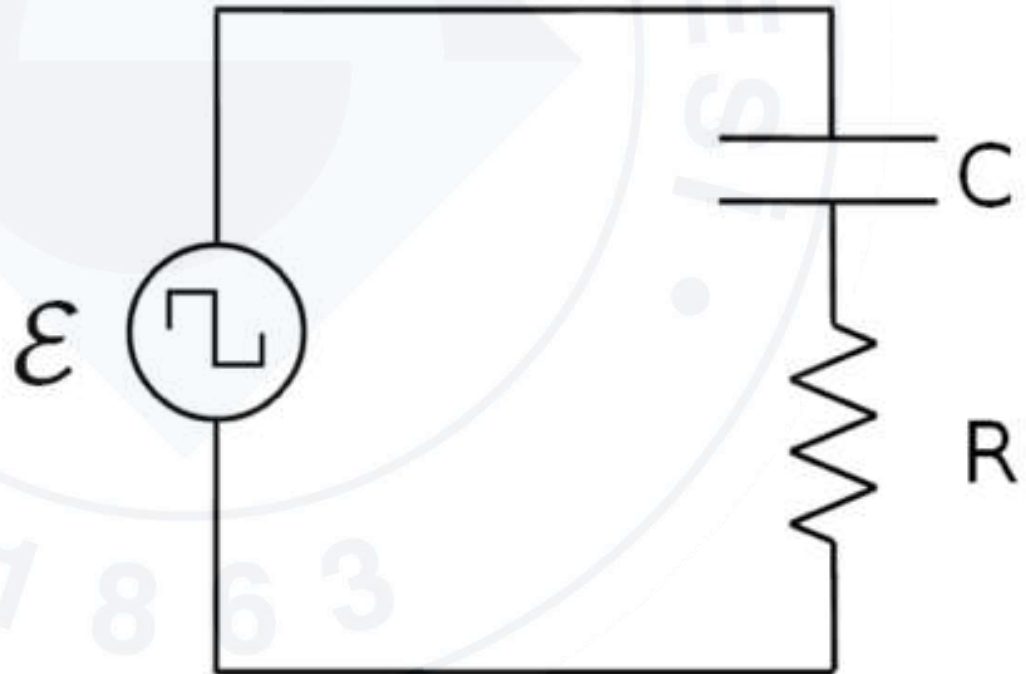
$$V_c = V_0 e^{-t/RC}$$

when  $V_c = V_0/2$

$$t = t_{1/2} = \ln 2 R_{tot} C$$

RC is the time constant

*here R is the total resistance in the circuit*



# CHARACTERISTICS OF A CAPACITOR

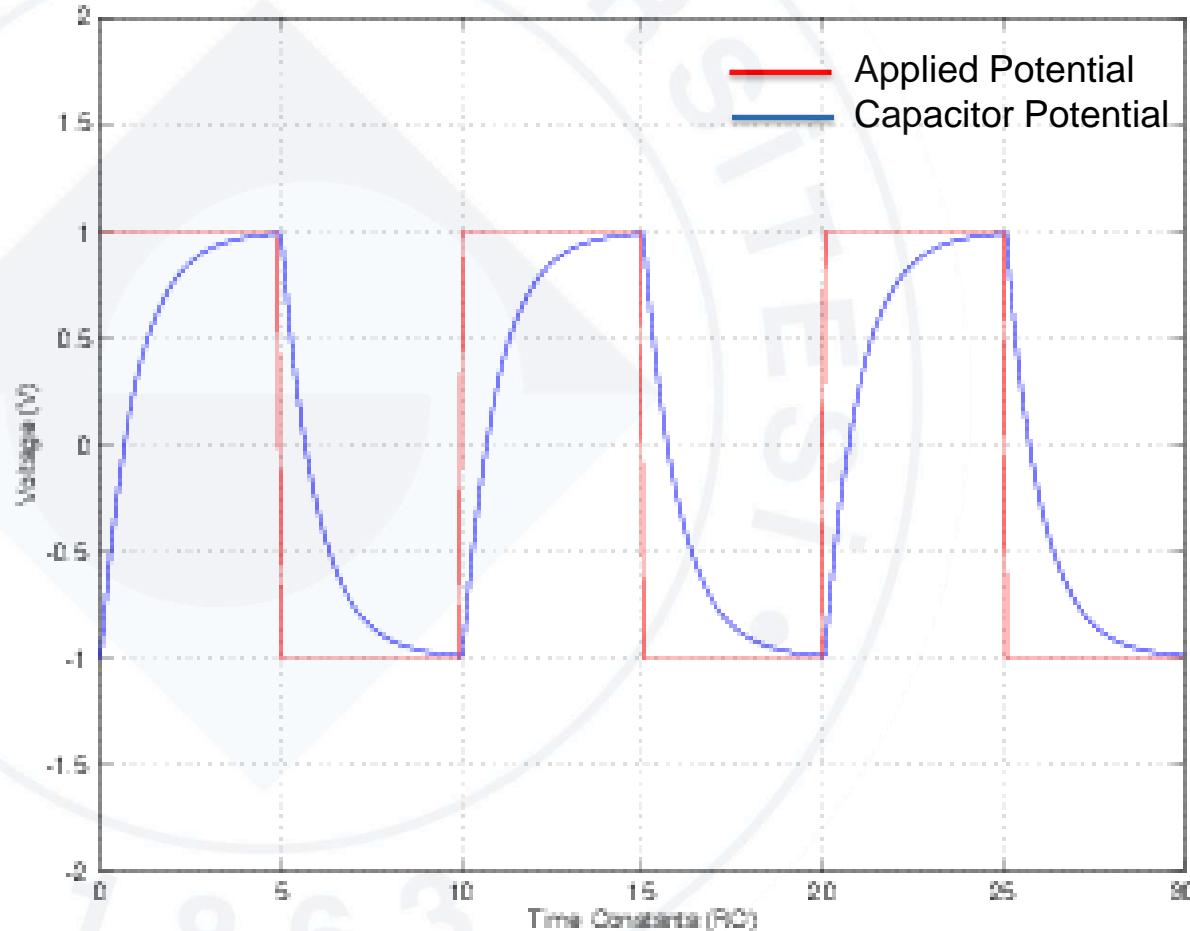
If we apply a square wave signal, choosing a period  $T$  much longer than the half-life of the RC circuit or

$$T \gg RC$$

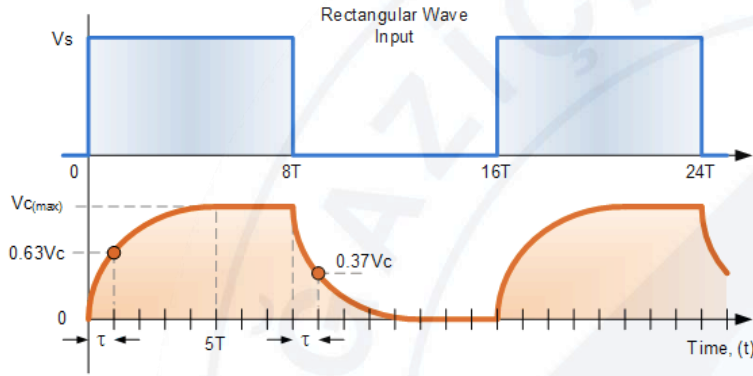
the RC time constant,

$$t_{1/2} = (\ln 2) R_{\text{tot}} C$$

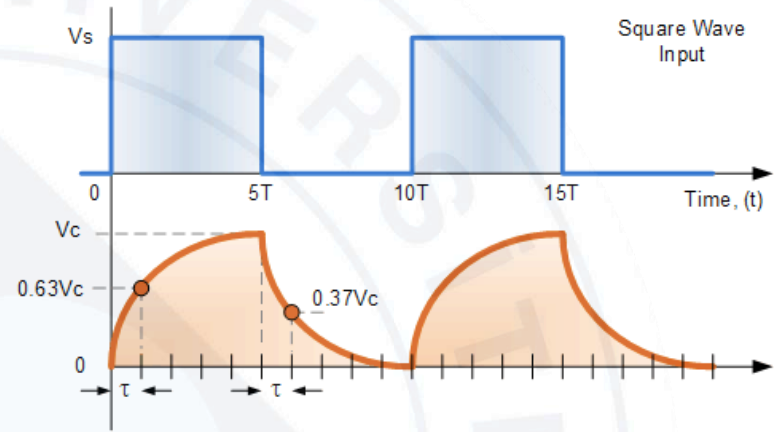
we get a waveform repeatedly displaying the charging and discharge of the capacitor when the square wave goes up and down.



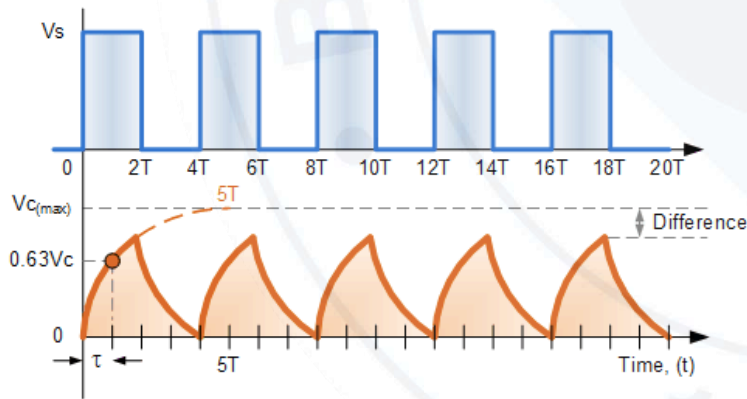
# CHARACTERISTICS OF A CAPACITOR



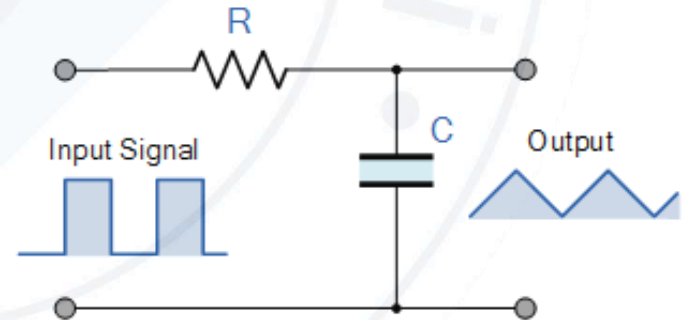
**Period = 16 RC,  $T > RC$**



**Period = 10 RC,  $T > RC$**



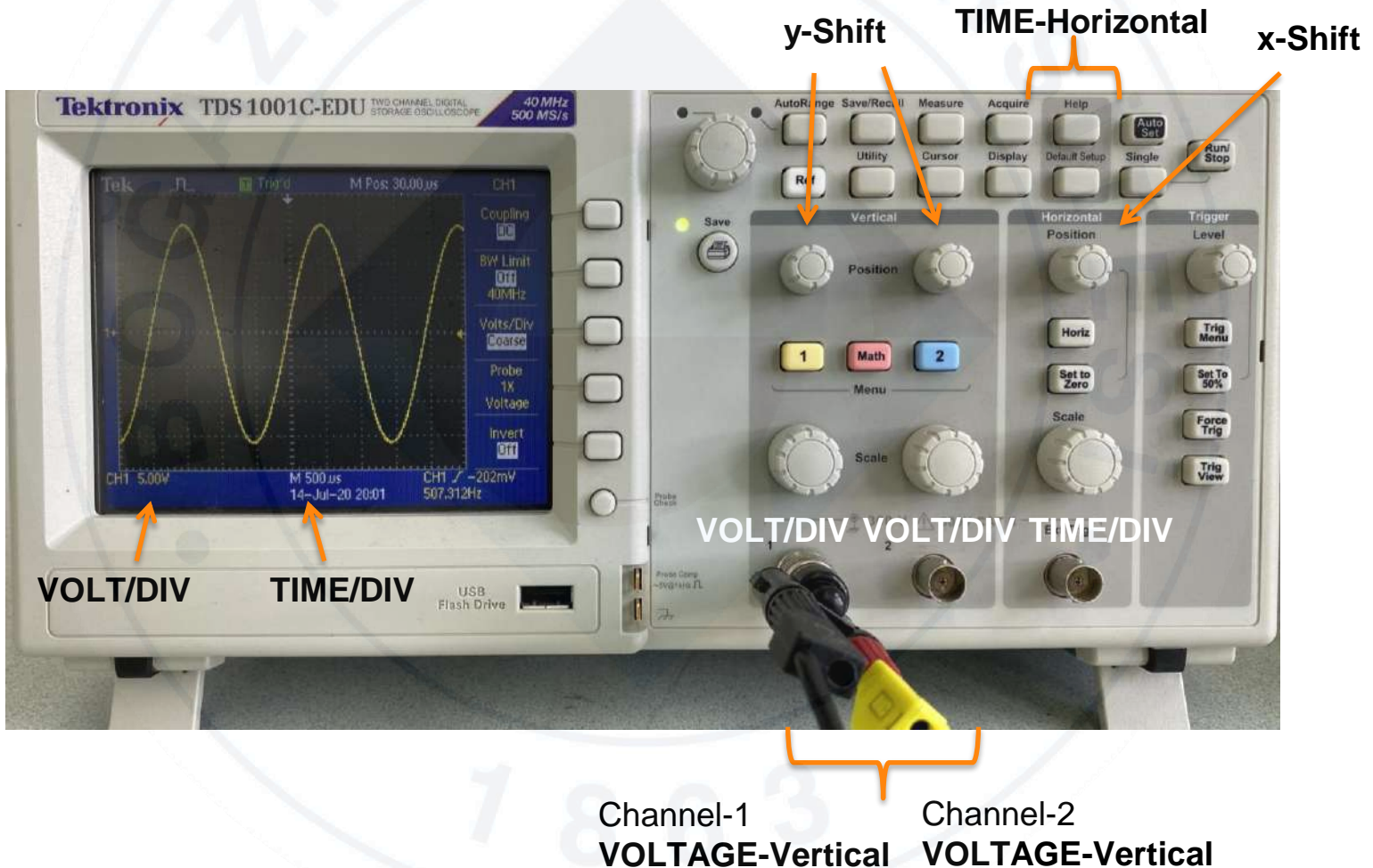
**Period = 4 RC,  $T > RC$**



**$T \ll RC$**

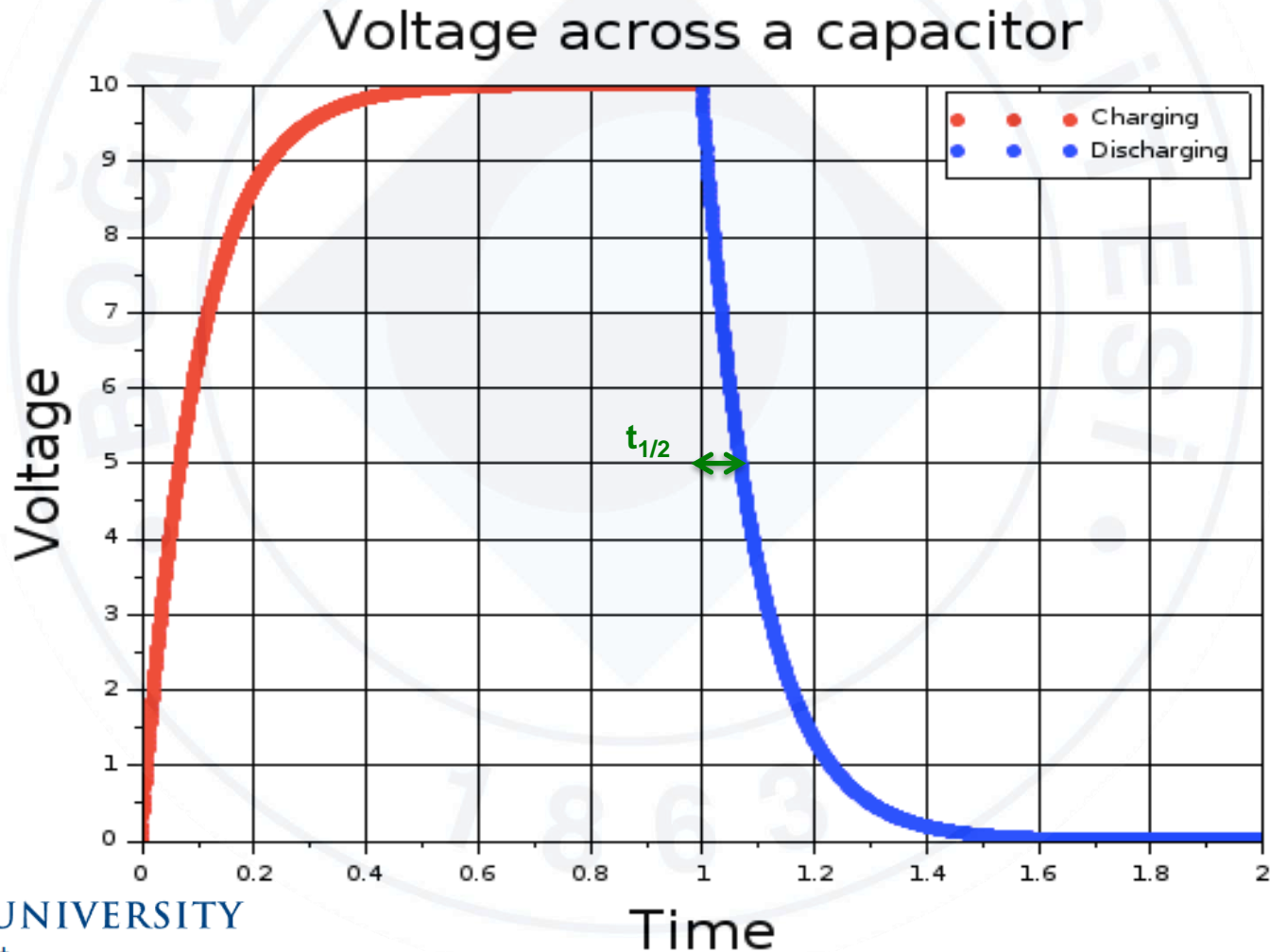
# CHARACTERISTICS OF A CAPACITOR

Oscilloscopes display the change of an electrical signal over time, with voltage and time as the Y- and X-axes, respectively, on a calibrated scale.



# CHARACTERISTICS OF A CAPACITOR

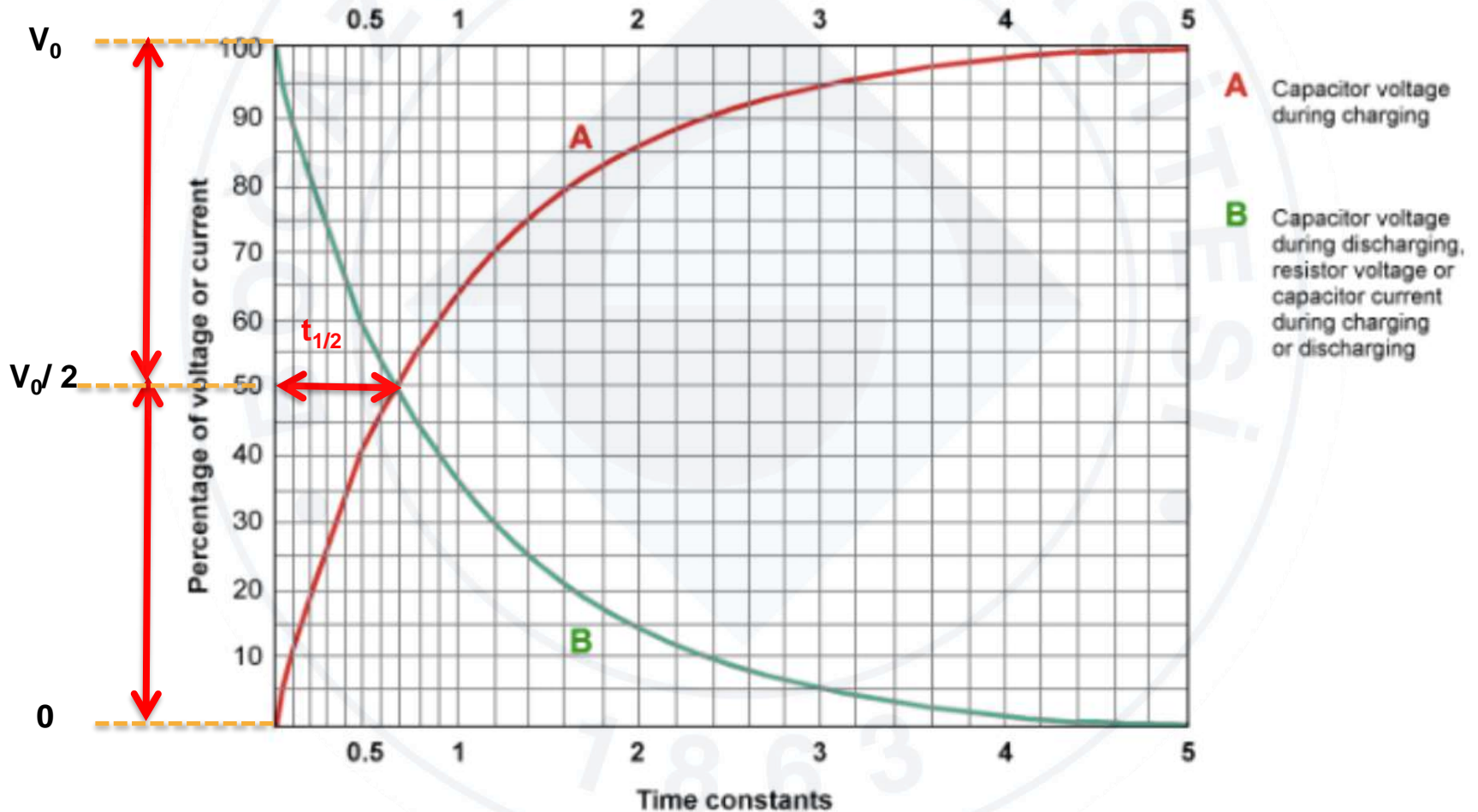
Measurement of half life of the capacitor:  
time needed to discharge half of the capacitor potential





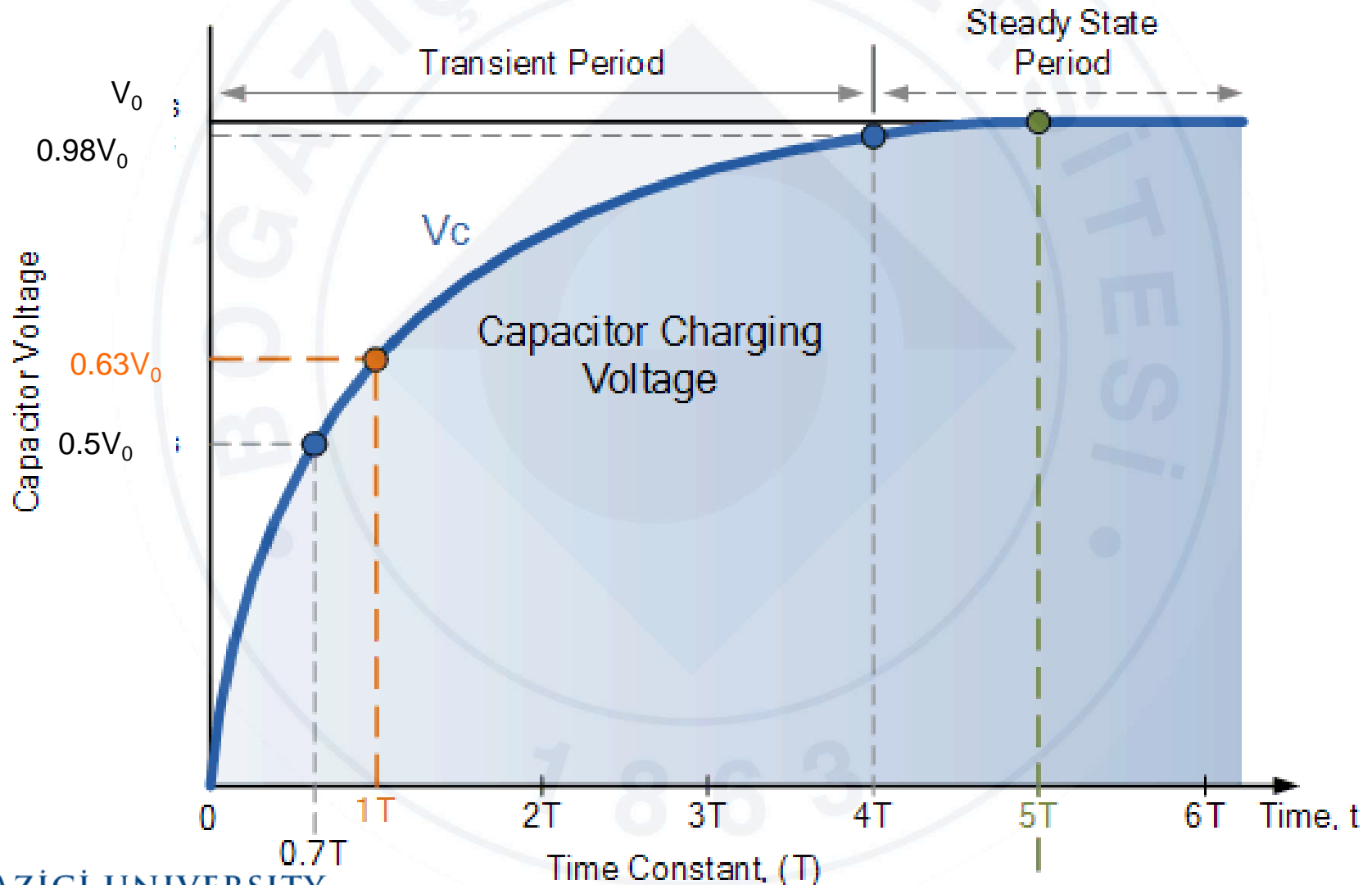
# CHARACTERISTICS OF A CAPACITOR

## Half-life of the Capacitor



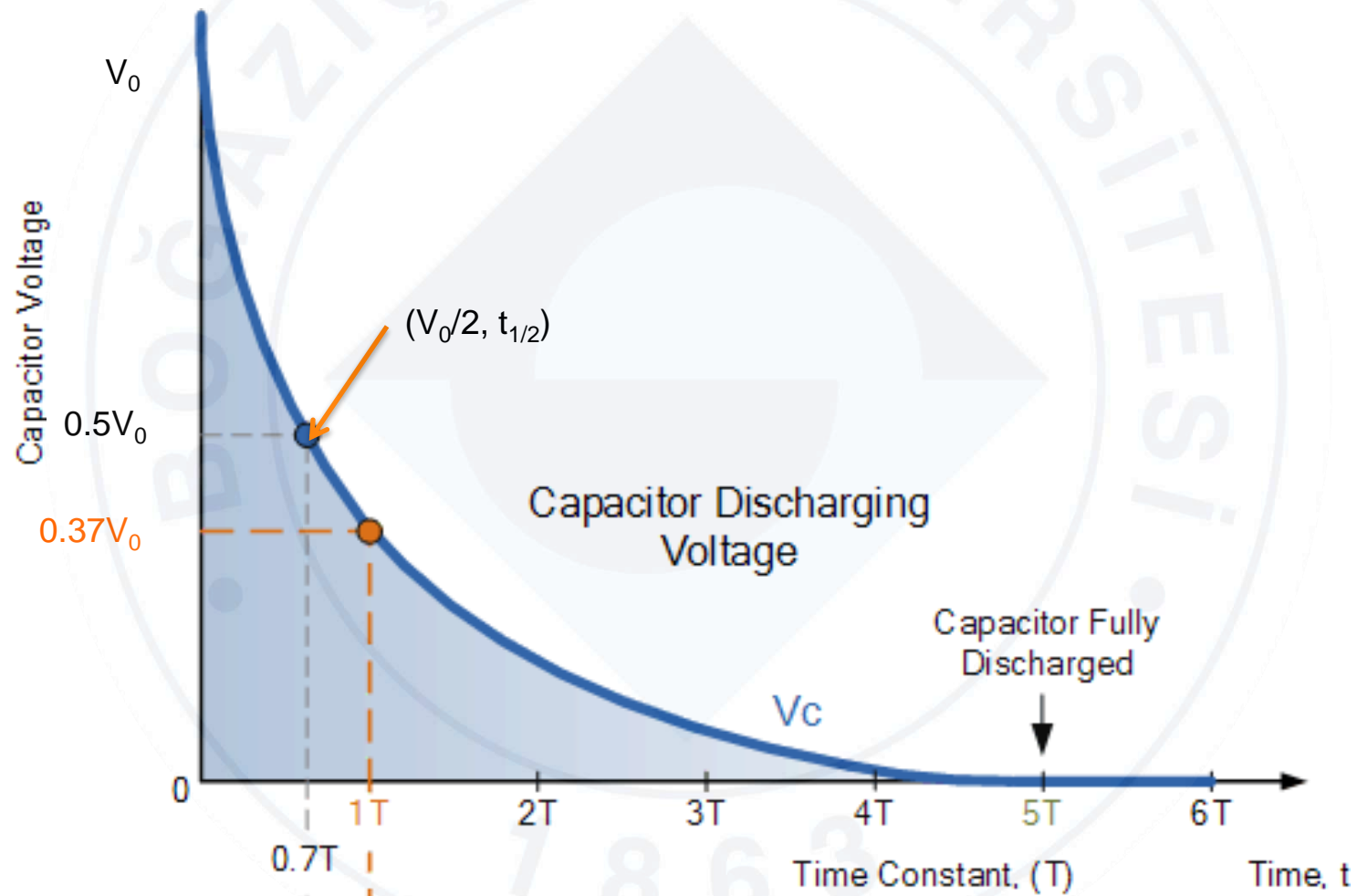
# CHARACTERISTICS OF A CAPACITOR

## Charging of the Capacitor



# CHARACTERISTICS OF A CAPACITOR

## Discharging of a Capacitor

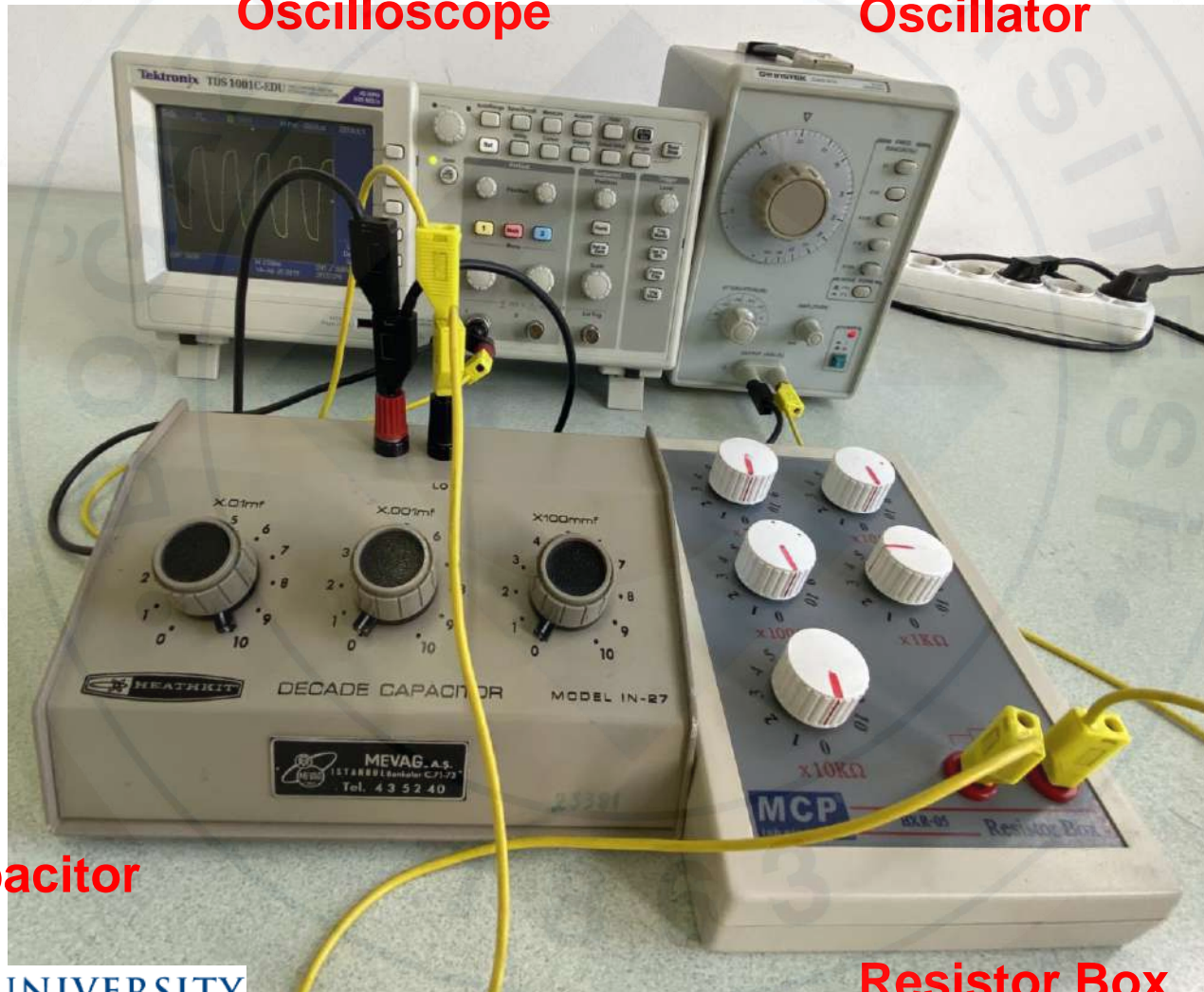


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# **SETUP AND EXPERIMENT**

# CHARACTERISTICS OF A CAPACITOR

## CIRCUIT

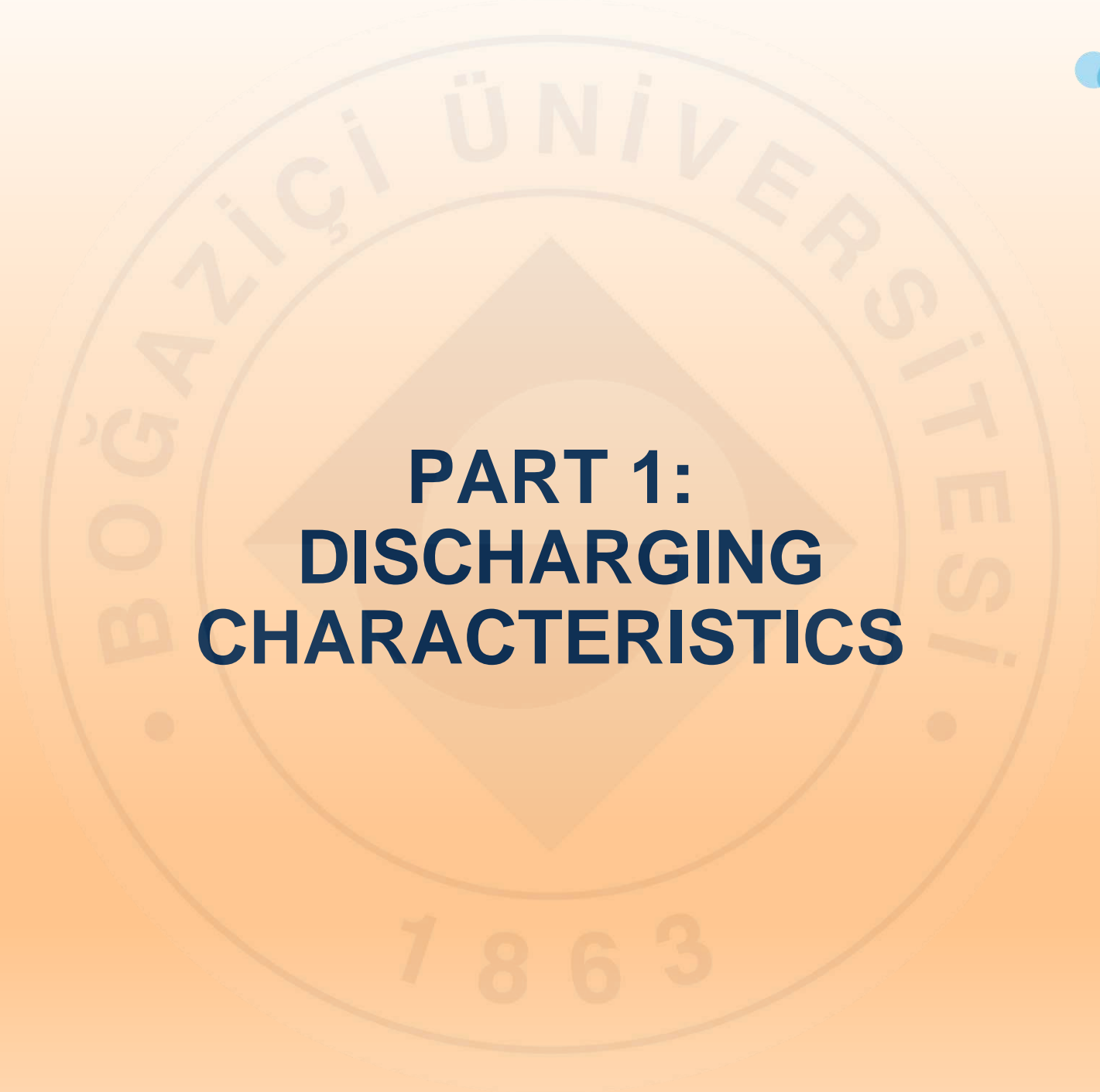


Oscilloscope

Oscillator

Capacitor

Resistor Box

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# **PART 1: DISCHARGING CHARACTERISTICS**

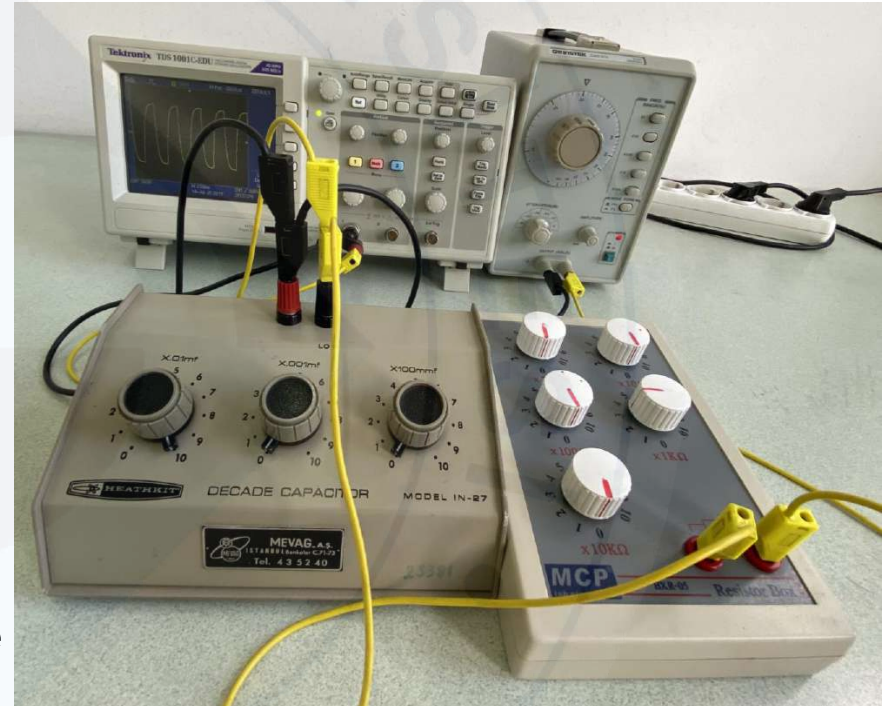
# CHARACTERISTICS OF A CAPACITOR

## An overview

**Given:** Resistance to set on Resistance box,  $R$ ; Internal resistance of SWG,  $R_{SWG}$ ; Capacitance,  $C$ .

**What to read:** half-life in cm,  $t_{1/2EV}(\text{cm})$ ; [VOLT/DIV]; [TIME/DIV].

**What to calculate:** Period of the SWG to be set,  $T$ ; frequency of the SWG,  $f_{TV}$ ; half-life in sec,  $t_{1/2}(\text{s})$ ; % error for half-life in sec  $t_{1/2}(\text{s})$ .



# CHARACTERISTICS OF A CAPACITOR

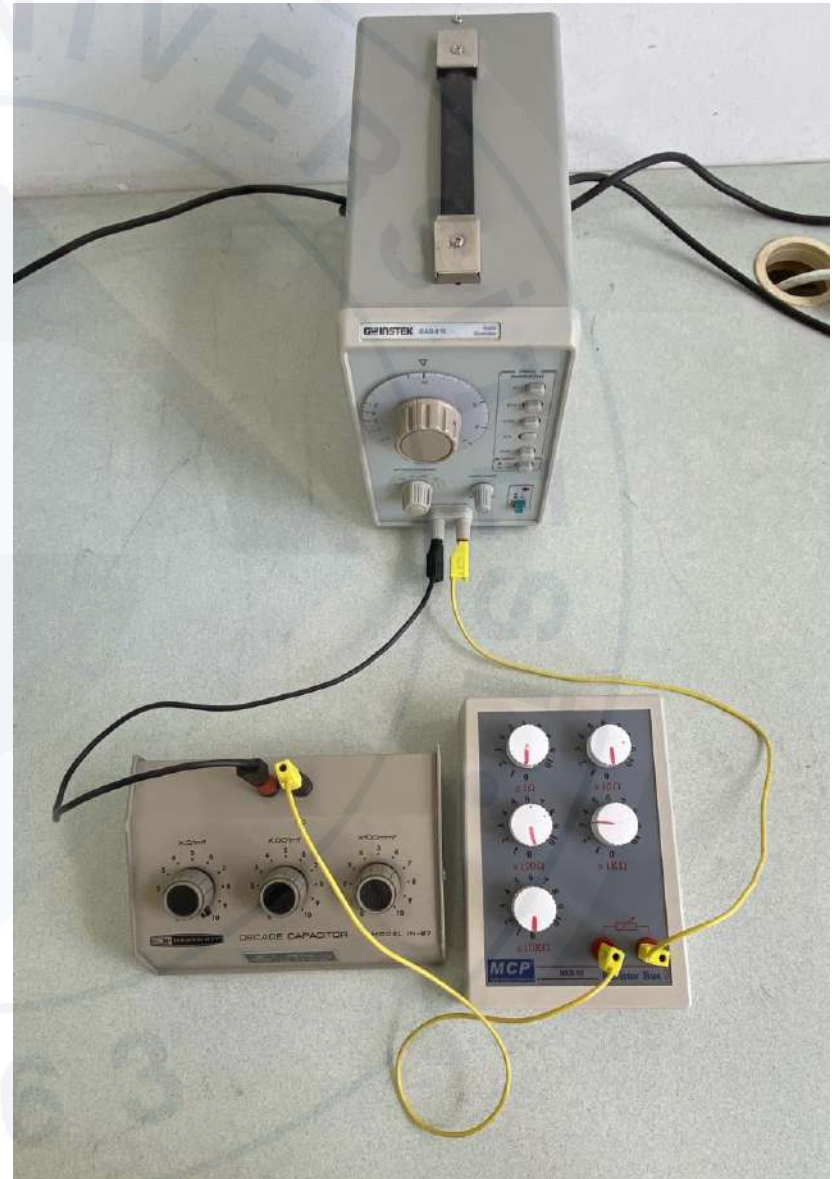
## CIRCUIT:

R and C are given in the Lab Report.

Internal resistance of Oscillator (Square Wave Generator) is  $600\Omega$ .

The resistance of the circuit will be the total resistance, the sum of R (resistor) and the internal resistance of the SWG.

Calculate the true value of the half-life of the RC circuit and determine the square wave frequency to set.





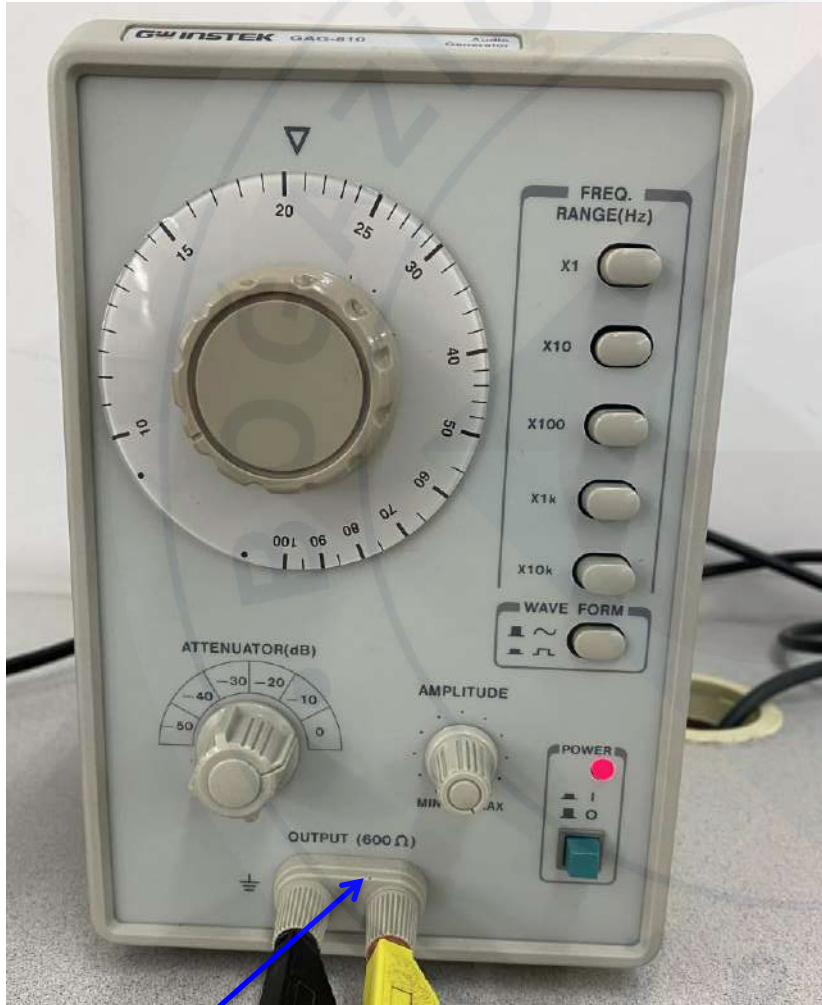
# CHARACTERISTICS OF A CAPACITOR

**CAPACITOR:** Set to  $0.1\mu\text{F}$  (here on the device **mf** means  $\mu\text{F}$ ).



# CHARACTERISTICS OF A CAPACITOR

## Oscillator (SWG)



Internal resistance,  $R_{SWG} = 600 \Omega$

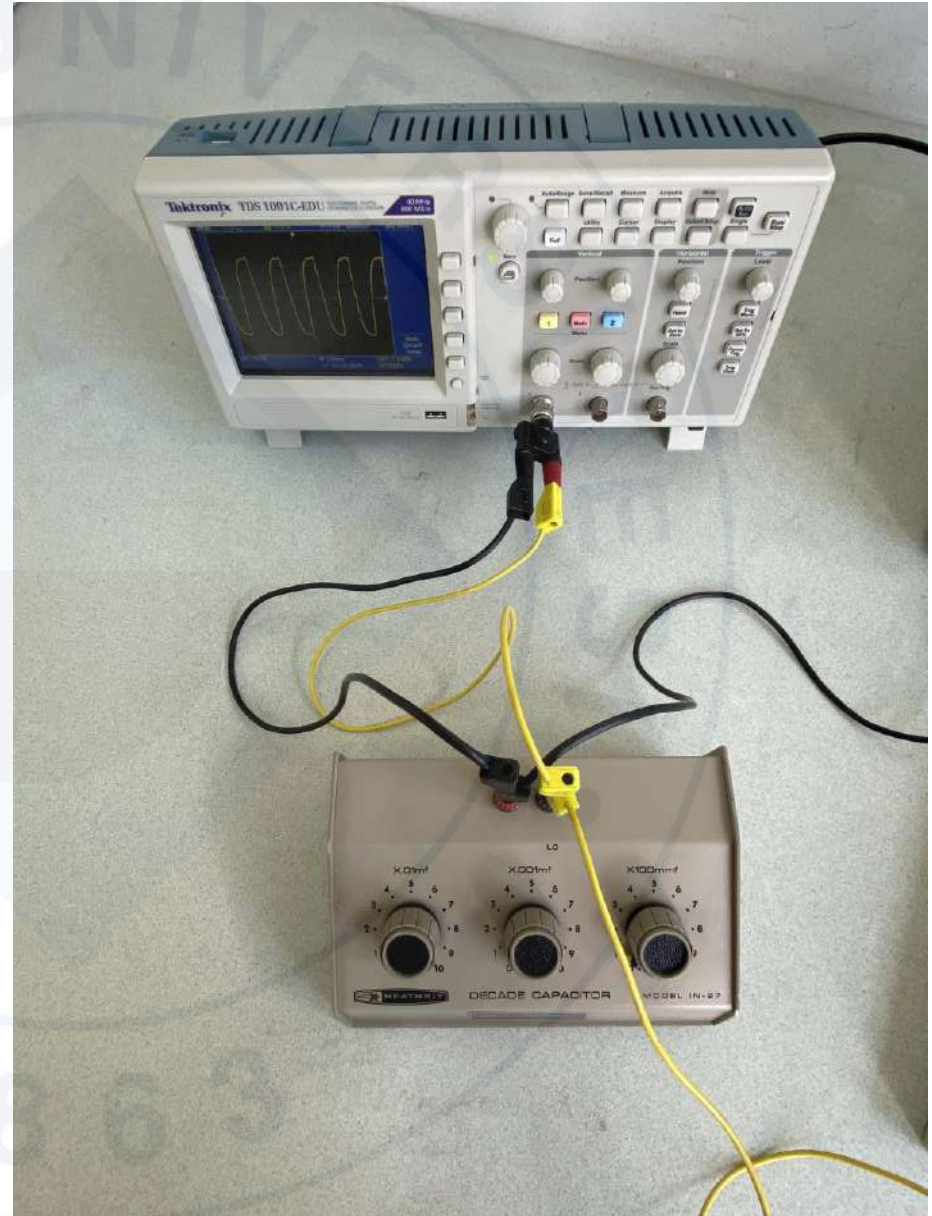
## Resistor Box



$R = 3000 \Omega$  is set

## CHARACTERISTICS OF A CAPACITOR

Oscilloscope is connected across (in parallel to) the capacitor to display the capacitor potential.



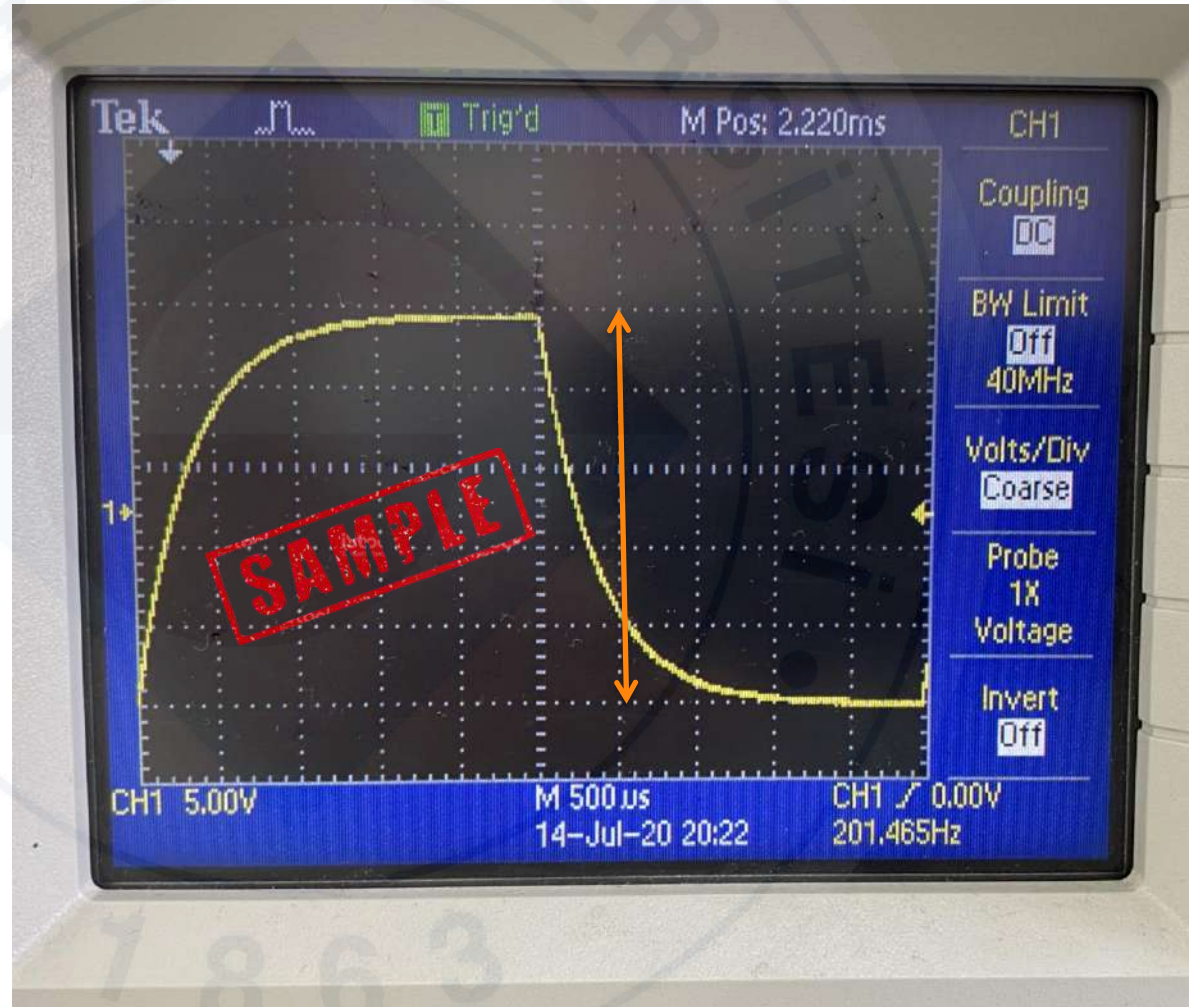
## CHARACTERISTICS OF A CAPACITOR

- Calculate the square wave frequency to set to the oscillator.

$R_T$ ,  $C$  is known.

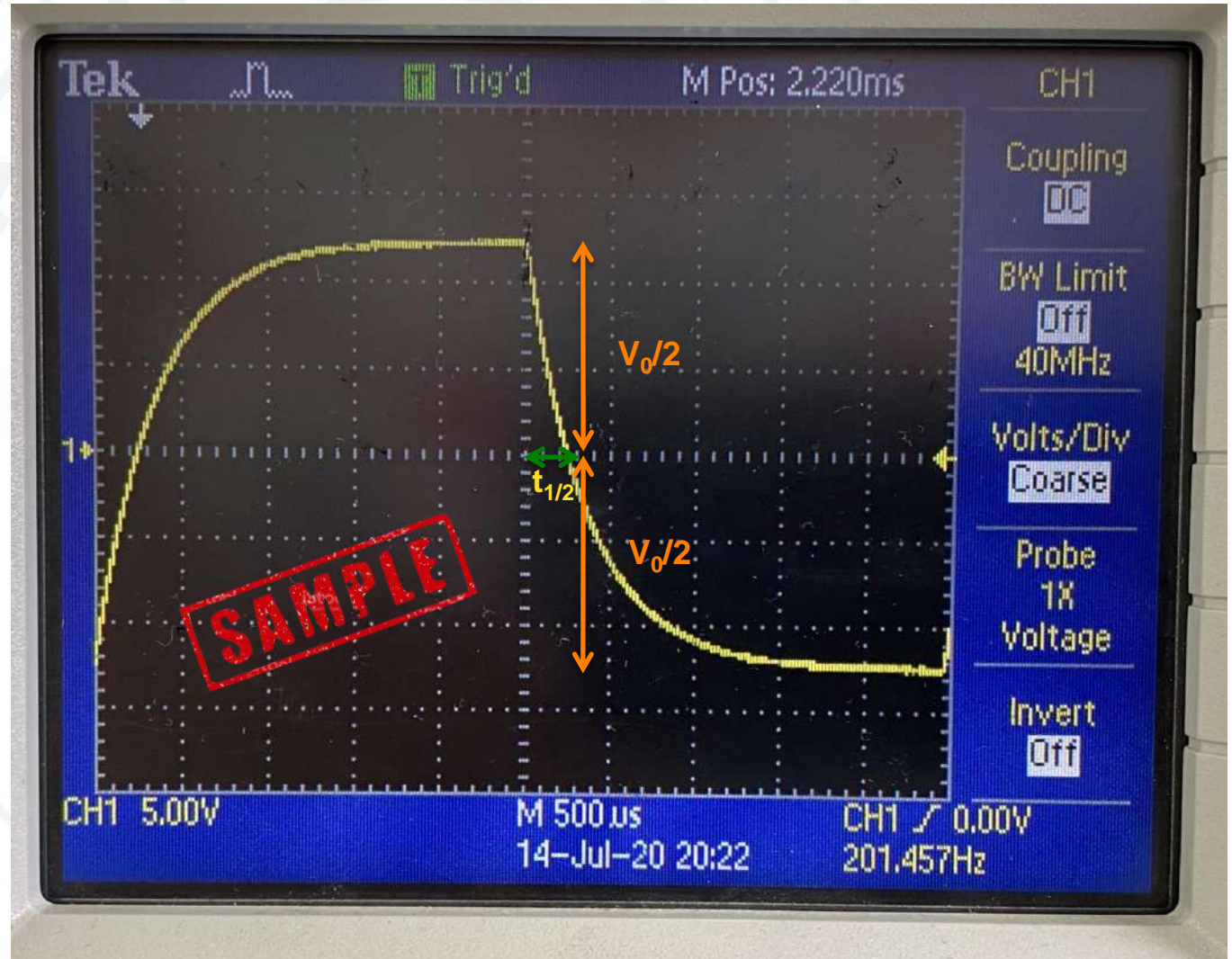
Calculate  $t_{1/2}$ .  $T=20 t_{1/2}$  is given. Determine  $T$  and  $f$ .

- TIME/DIV and VOLT/DIV knobs are set to display one charging and one discharging phase on the oscilloscope screen.



# CHARACTERISTICS OF A CAPACITOR

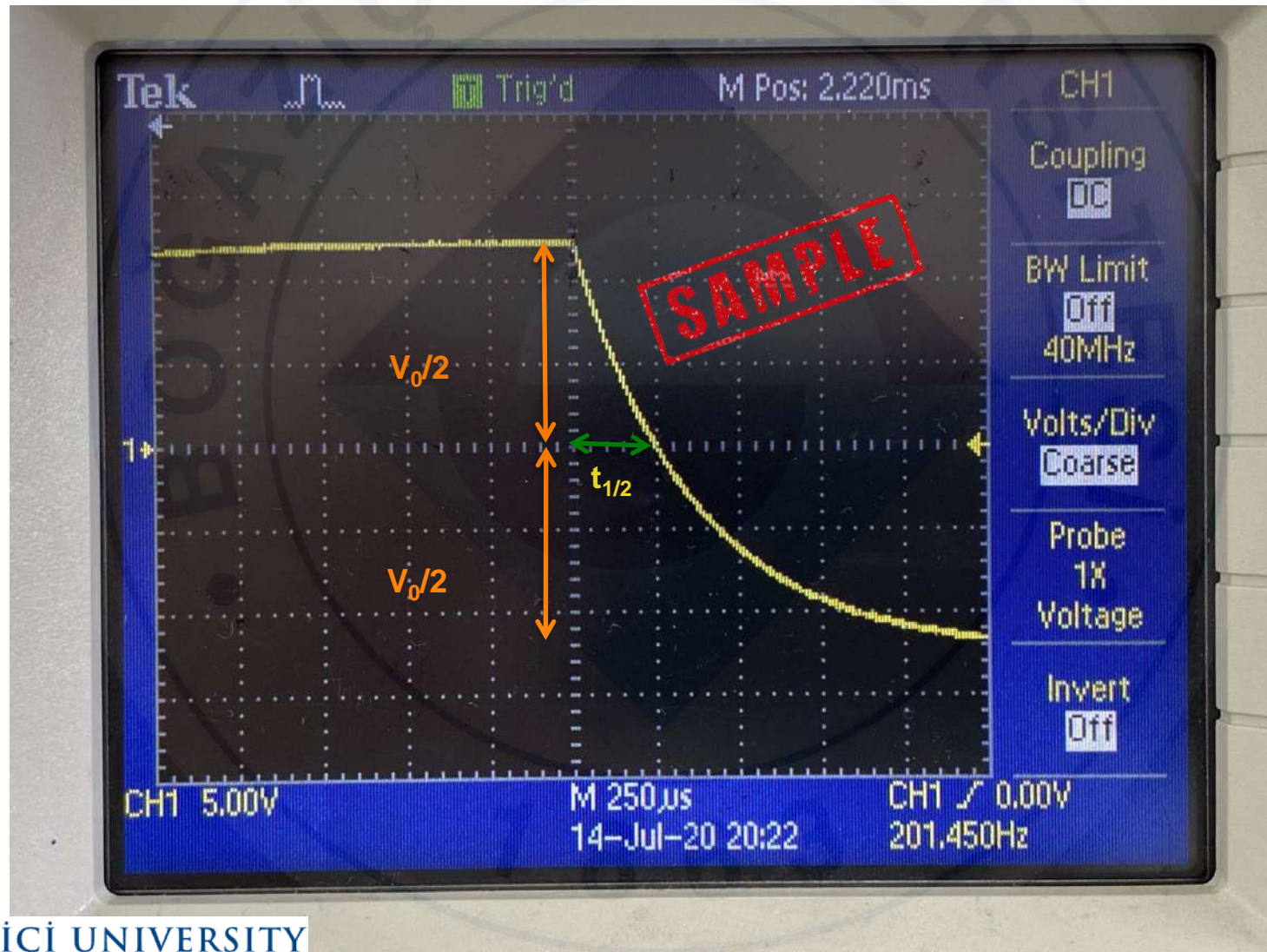
- From the observed pattern on the oscilloscope screen, measure  $t_{1/2}$ .  
But it is better to choose much better TIME/DIV setting.



- Calculate  $t_{1/2EV}$  using this measured  $t_{1/2EV}(cm)$ .

# CHARACTERISTICS OF A CAPACITOR

Half Life of Capacitor measurement with different TIME/DIV setting.



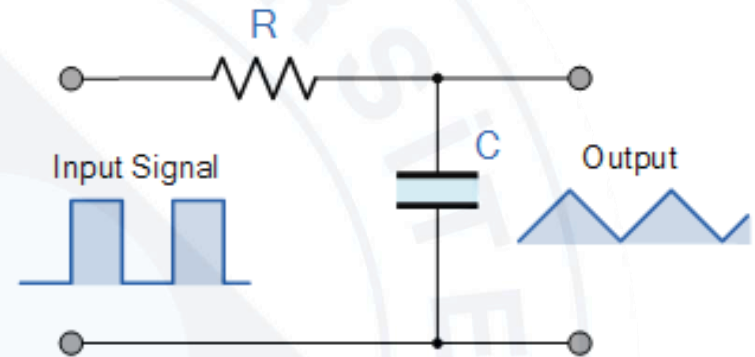
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# **PART 2: AN INTEGRATING CIRCUIT**

## CHARACTERISTICS OF A CAPACITOR

If we go to the other extreme and choose a square wave signal with a period much shorter than the RC time constant, then the voltage across the capacitor is basically the integral of the applied potential.

$$T \ll RC$$



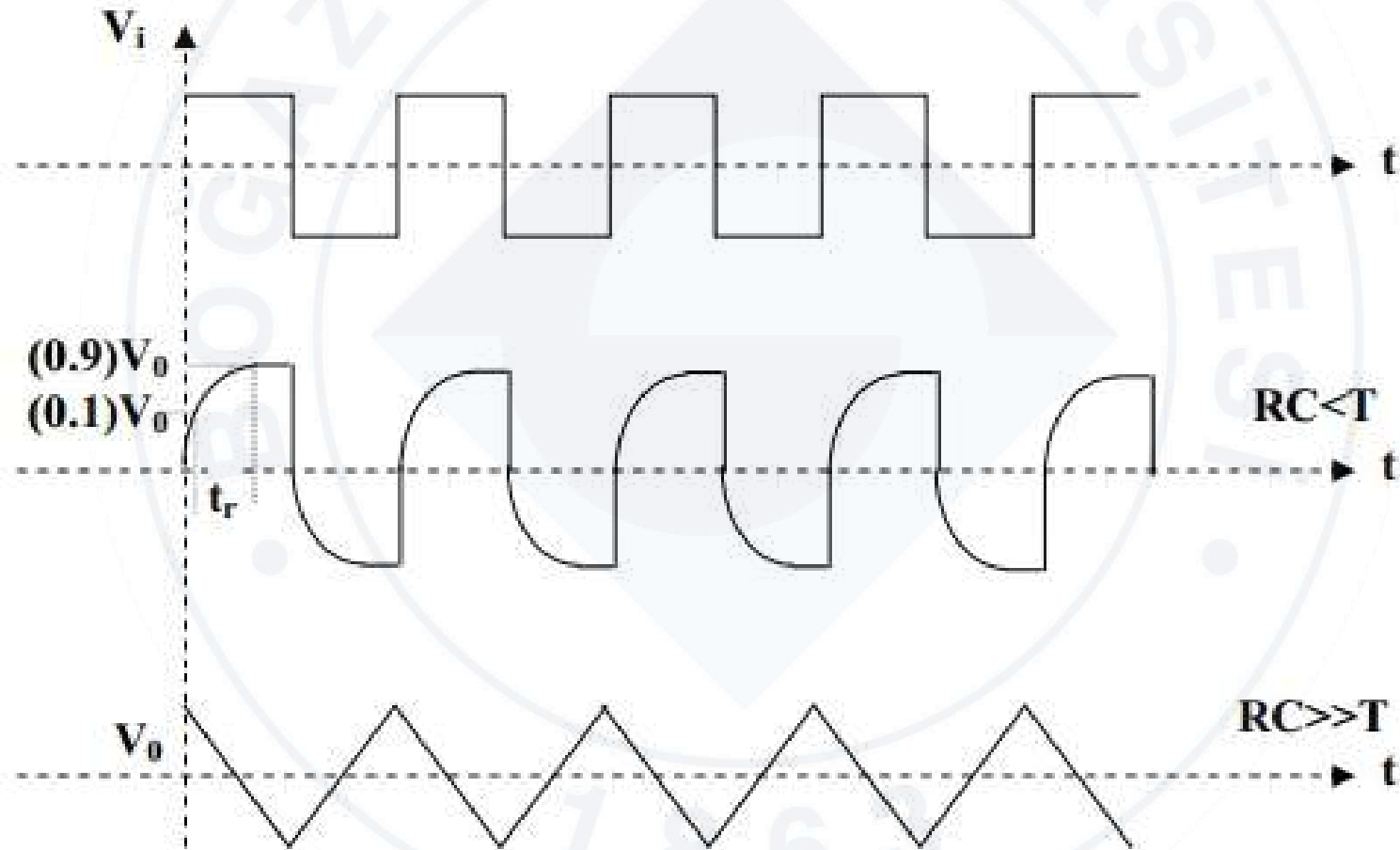
since  $V_C \ll V_R$

$$R \frac{dq}{dt} \approx V_{app} \Rightarrow \frac{dq}{dt} = \frac{V_{app}}{R} \quad \rightarrow \quad V_c = \frac{q}{C} = \frac{1}{RC} \int V_{app} dt$$



# CHARACTERISTICS OF A CAPACITOR

In this part we will study the case  $RC \gg T$ . In this case, the frequency of the oscillator (SWG) is set to a very high value. At high frequency circuit becomes an integrating circuit.



# CHARACTERISTICS OF A CAPACITOR

Use the same circuit, but set much higher frequency on the Square Wave Generator ( $20 \times 10^3$  Hz).



# CHARACTERISTICS OF A CAPACITOR

## Oscillator (SWG)



Internal resistance,  $R_{SWG} = 600 \Omega$

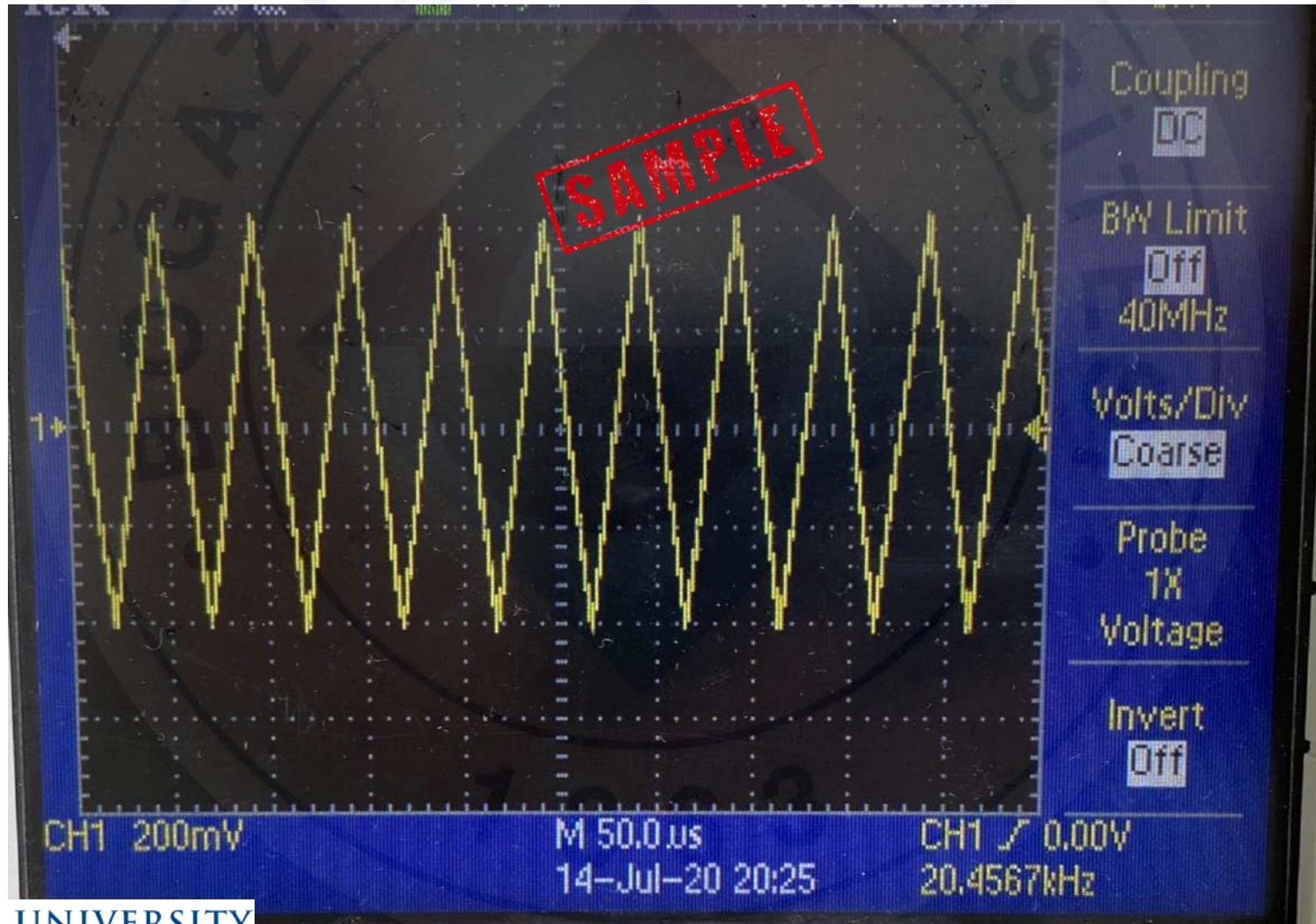
## Resistor Box



$R = 3000 \Omega$  is set

# CHARACTERISTICS OF A CAPACITOR

The controls (TIME/DIV and VOLT/DIV) are adjusted to for optimum focus.



# CHARACTERISTICS OF A CAPACITOR

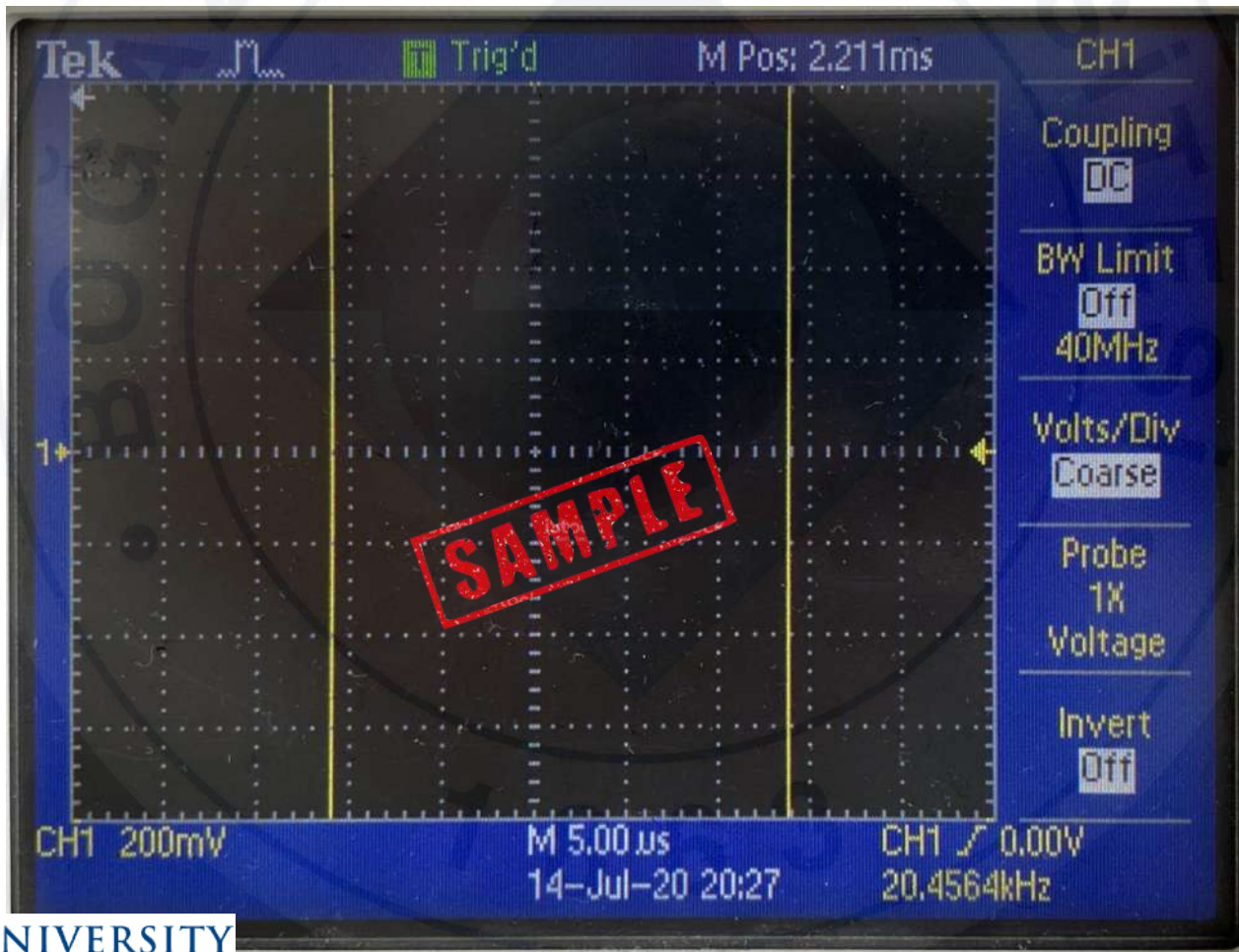
Draw one period of the voltage across the capacitor (the Capacitor Voltage Waveform) in your report.

Indicates the horizontal axis where the signal is zero.



## CHARACTERISTICS OF A CAPACITOR

Now, connect the oscilloscope directly to the square wave generator in order to observe the applied voltage. Since  $V_{app} \gg V_c$  we need to adjust the VOLT/DIV setting.



# CHARACTERISTICS OF A CAPACITOR

Draw one period of the applied square wave voltage by using the same scale you drew the corresponding pattern for the voltage across the capacitor ( $V_c$ ). Show that the capacitor voltage is proportional to the integral of the applied square wave voltage

Indicates the horizontal axis where the signal is zero.



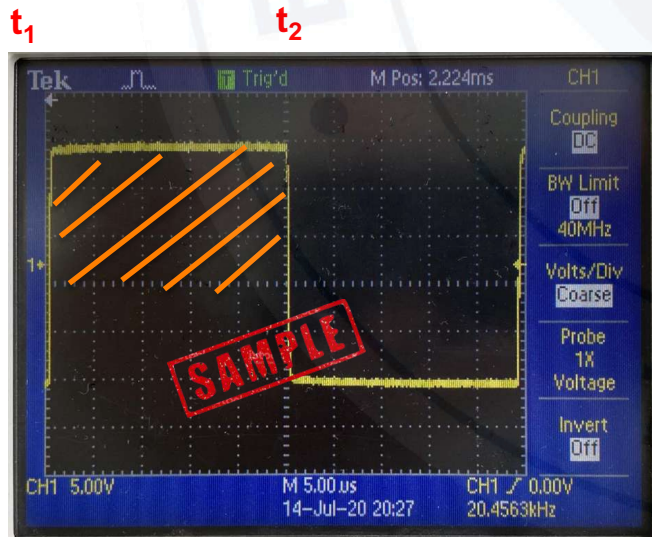
# CHARACTERISTICS OF A CAPACITOR

Show that the capacitor voltage is proportional to the integral of the applied square wave voltage.



$$V_c = V_{c2} - V_{c1}$$

$$V_c = \frac{q}{C} = \frac{1}{RC} \int V_{app} dt$$



$$\int V_{app} dt = (t_2 - t_1) V_{app}$$