



Boğaziçi University

**Introductory
Phys Labs**

1863

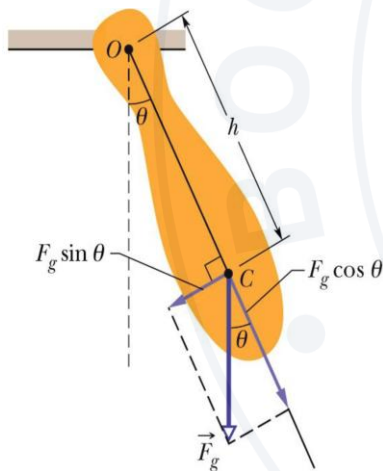
ANGULAR HARMONIC MOTION

PHYL102

1863

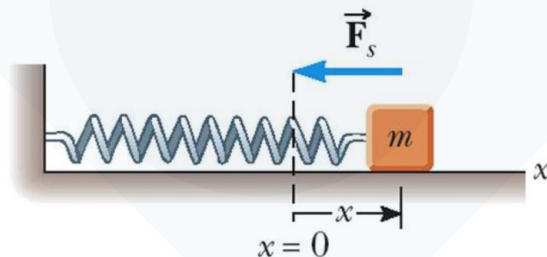
Simple harmonic motion is a special type of periodic motion where the restoring force on the moving object is directly proportional to the object's displacement magnitude and acts towards the object's equilibrium position.

Physical Pendulum



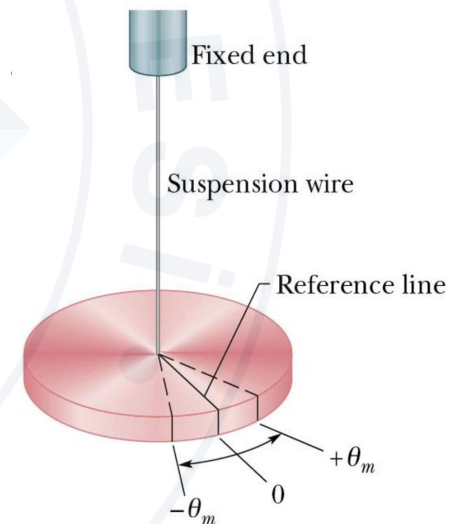
$$T = 2\pi \sqrt{\frac{I}{Mgh}}$$

Simple Harmonic Oscillator



$$T = 2\pi \sqrt{\frac{m}{k}}$$

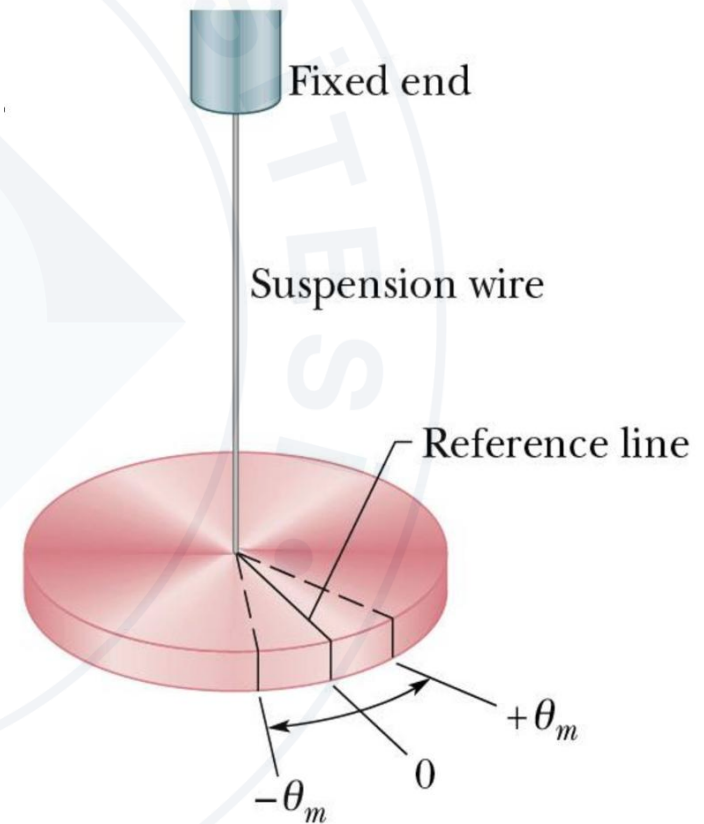
Torsional Pendulum



$$T = 2\pi \sqrt{\frac{I}{\kappa}}$$

ANGULAR SIMPLE HARMONIC MOTION

- The figure shows an angular version of simple harmonic oscillator. When a body is allowed to rotate freely about a given axis then the oscillation is known as the angular oscillation.
- The particle or the body undergoes small angular displacement about mean position. This results, when the body under stable equilibrium is disturbed by a small external torque.
- A *torsional pendulum* consists of a disk suspended from a wire, which is then twisted and released, resulting in an oscillatory motion.

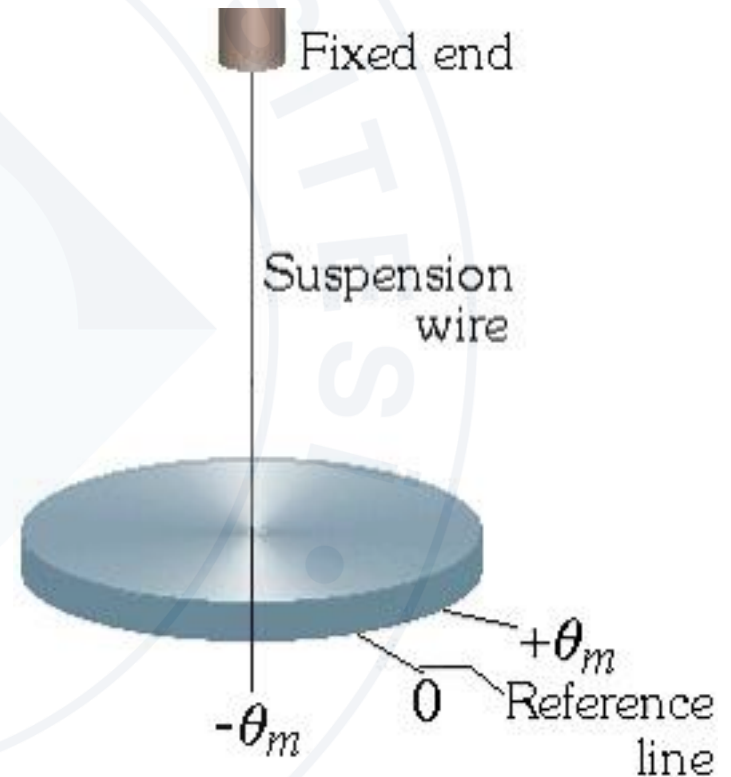


The oscillatory motion is caused by a restoring torque which is proportional to the angular displacement,

$$\tau = I\alpha = -\kappa\theta$$

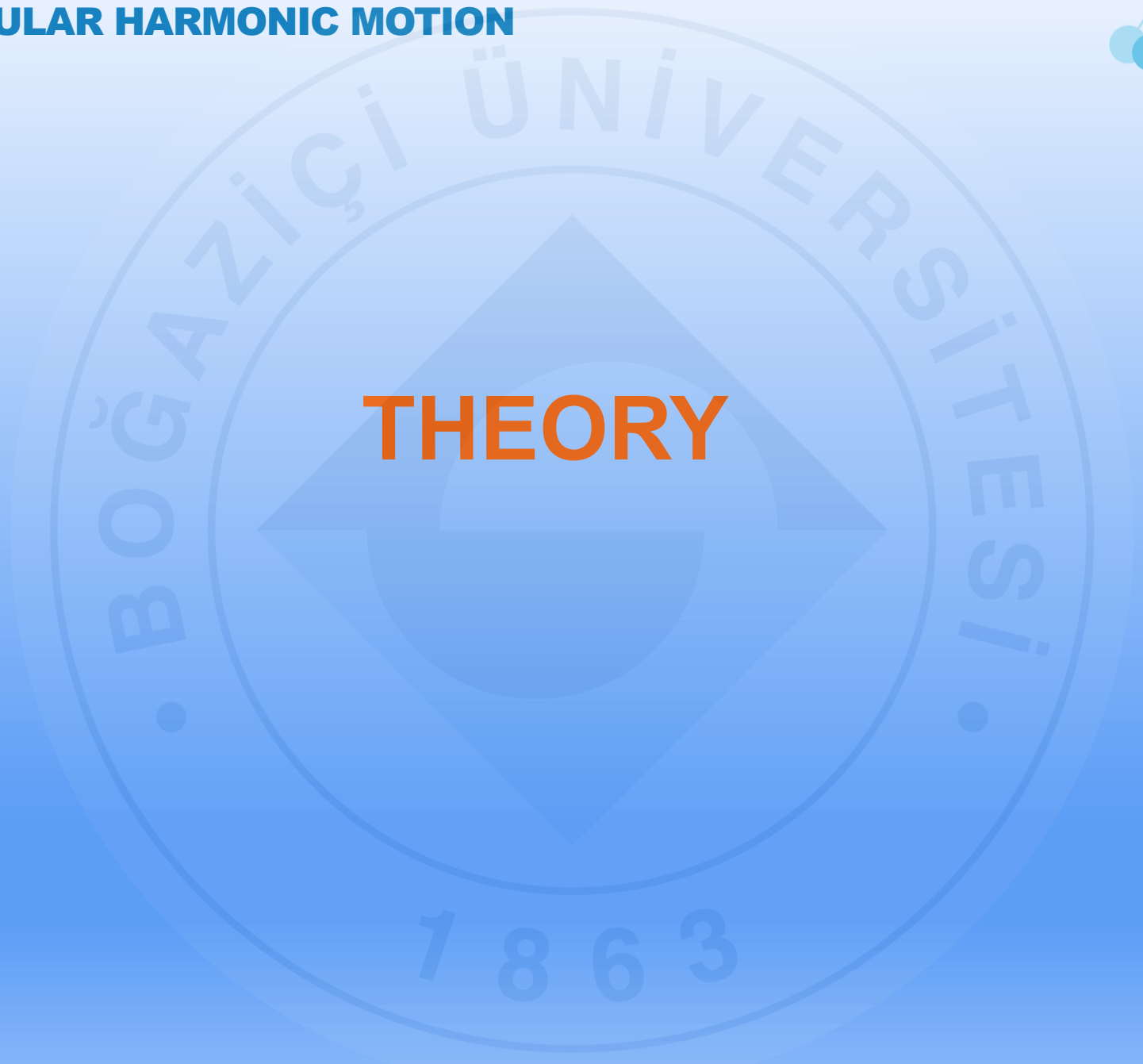
(Angular form of Hooke's law)

Where κ is the torsion constant that depends the length, diameter and material of suspension wire. I is the rotational inertia of the object about twisting axis and α is the angular acceleration of the object.



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THEORY



EQUATION OF MOTION:

$$\tau = I\alpha = -\kappa\theta$$

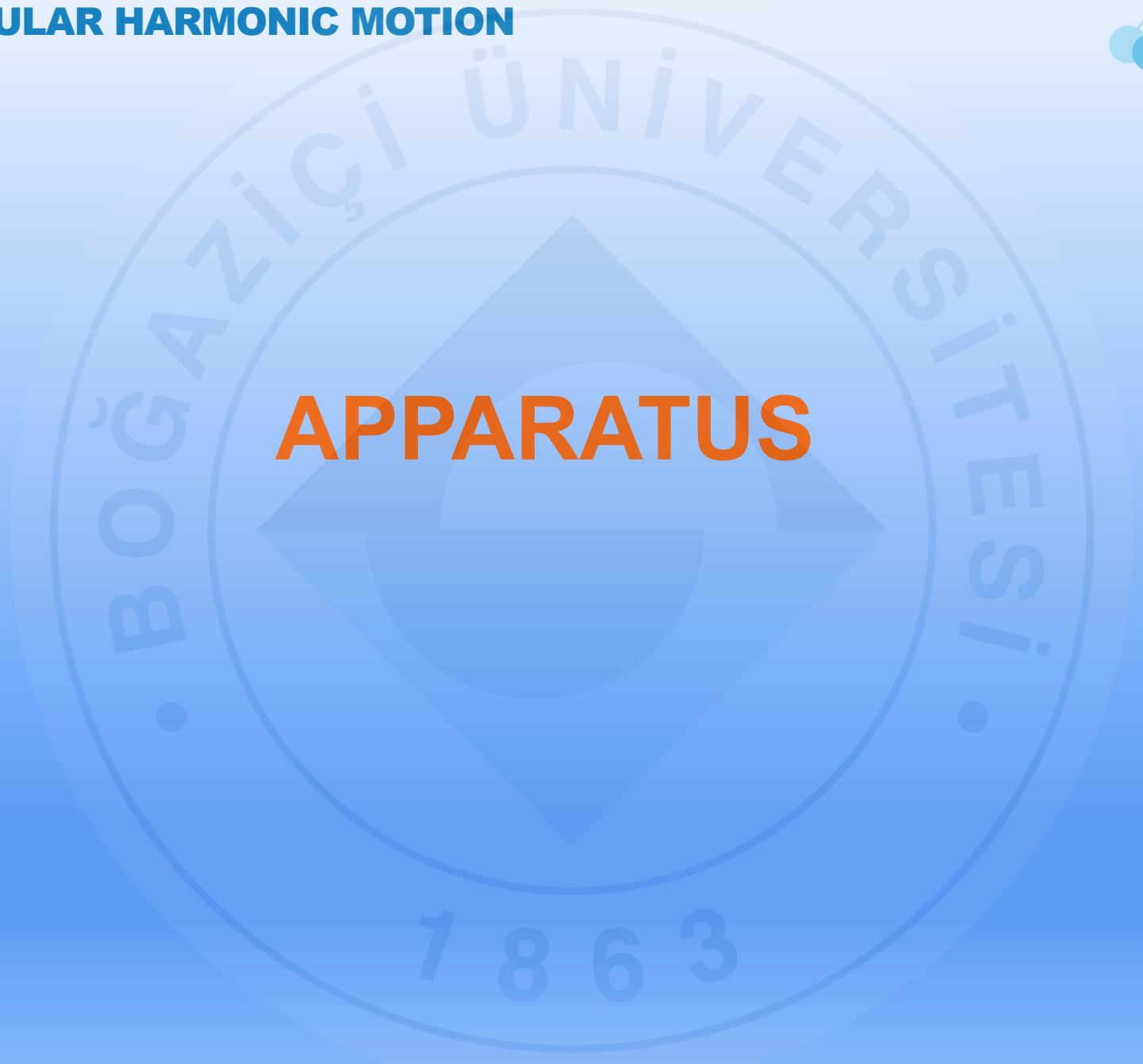
Angular acceleration $\alpha = \frac{d^2\theta}{dt^2}$

$$I\frac{d^2\theta}{dt^2} = -\kappa\theta \quad \rightarrow \quad \frac{d^2\theta}{dt^2} + \frac{\kappa}{I}\theta = 0 \quad \rightarrow \quad \frac{d^2\theta}{dt^2} + \omega^2\theta = 0$$

Where $\omega^2 = \frac{\kappa}{I}$ $\omega = \sqrt{\frac{\kappa}{I}}$ $T = \frac{2\pi}{\omega}$

$$T = 2\pi\sqrt{\frac{I}{\kappa}}$$

APPARATUS



ANGULAR HARMONIC MOTION



Ring

$$I_{ring} = \frac{1}{2} M \left[(\bar{R}_{inner})^2 + (\bar{R}_{outer})^2 \right]$$

Torsional
wire

Disk

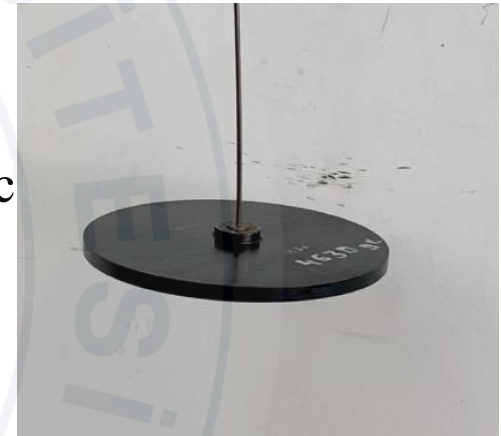
$$I_{disk} = \frac{MR^2}{2}$$

EXPERIMENT



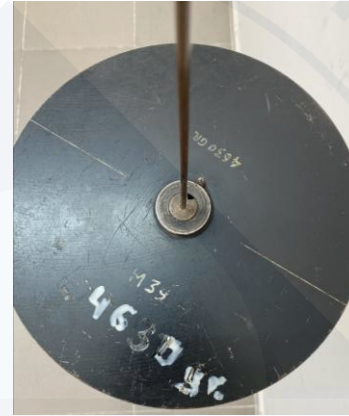
OBJECTIVE: To find the moment of inertia of the ring and compare result with theoretical value

- **PART I:**
 - Measure the period of disc
 - Calculate the moment of inertia of the disc
 - Find the torsion constant K
- **PART II:**
 - Measure the period of the disc and the ring together
 - Calculate the total moment of inertia of (disc + ring)
 - Find the experimental value of the moment of the inertia of the ring

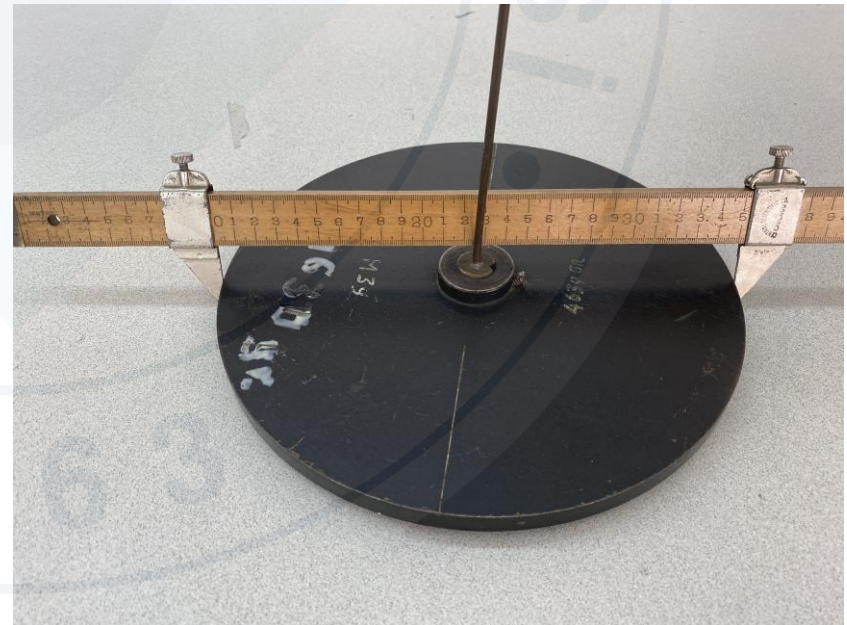
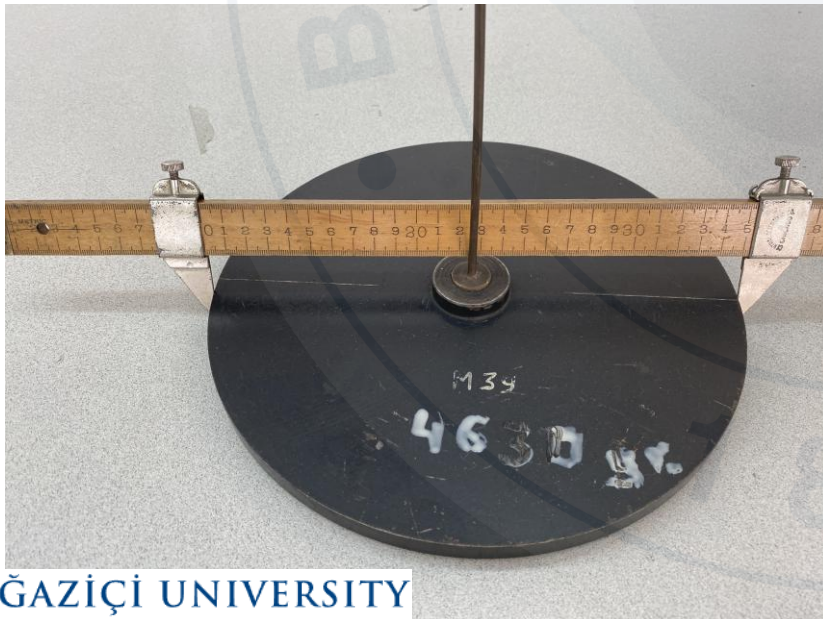


Theoretical value of the moment of inertia of the Disc:

$$I_{\text{disk}} = \frac{MR^2}{2}$$



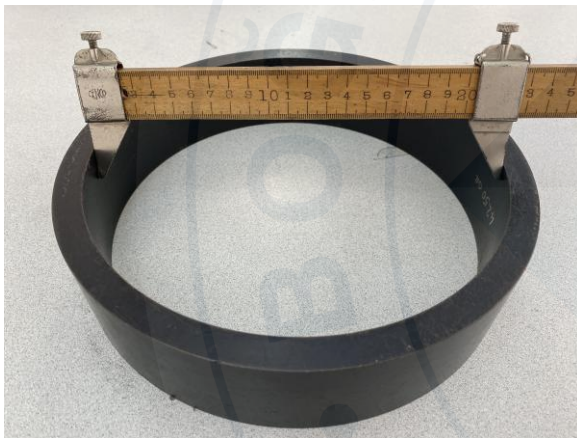
SAMPLE



Theoretical value of the moment of inertia of the Ring:

$$I_{ring} = \frac{1}{2} M \left[(\bar{R}_{inner})^2 + (\bar{R}_{outer})^2 \right]$$

SAMPLE



PART I

Use stopwatch to measure the time, t , for the disc to complete 20 oscillations, and determine the mean period of oscillation T .

$$T = 2\pi \sqrt{\frac{I}{\kappa}} \rightarrow I_{disc} = \frac{MR^2}{2}$$

compute κ torsion constant of the rod.



PART II

Place the ring whose moment of inertia is unknown, on the disc. Use stopwatch to measure the time to complete 20 oscillations, and determine the mean period of oscillation T .

$$T = 2\pi \sqrt{\frac{I_{total}}{\kappa}}$$

Compute the sum of the moments of inertia of the disc and the ring.



PART II

$$T = 2\pi \sqrt{\frac{I_{total}}{\kappa}}$$

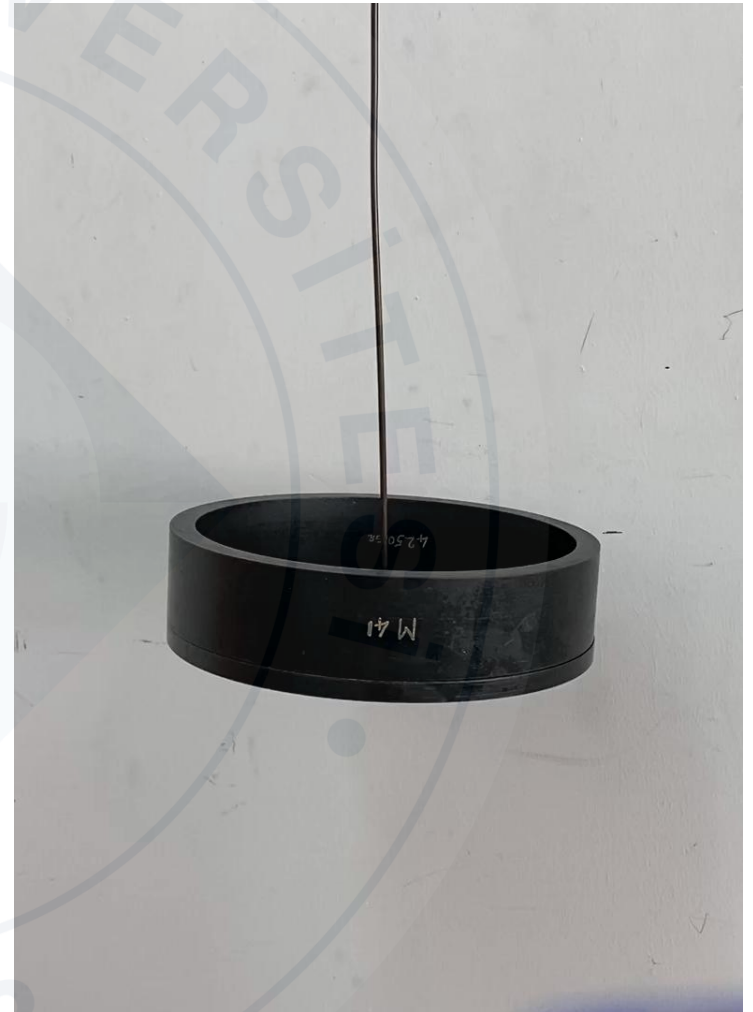
Total moment of inertia is equal to

$$I_{total} = I_{disc} + I_{ring}$$

Experimental value of the moment of inertia of the **ring**:

$$I_{ring} = I_{total} - I_{disc}$$

Compute the theoretical value of moment of inertia and determine the percentage error.



ANGULAR HARMONIC MOTION

Measure & read or calculate the following values

Part 1: Moment of Inertia of the Disk (1 p)

Time for 20 oscillations	t	
Period for one oscillation	T	
Diameter of the disk	D_{disk}	
Radius of the disc	R_{disk}	
Mass of the disc	M_{disk}	

Take the data and fill in the table for the DISC.

ANGULAR HARMONIC MOTION

Part 2: Moment of Inertia of the Ring & Disc (1.4 p)

Time for 20 oscillations	t^*	
Period for one oscillation	T	
Outer diameter of the ring	D_{outer}	
Outer Radius of the ring	R_{outer}	
Inner diameter of the ring	D_{inner}	
Inner Radius of the ring	R_{inner}	
Mass of the ring	M_{ring}	

Take the data, fill in the table for the Disc + Ring.

ANGULAR HARMONIC MOTION

Calculate the following quantities (Show your formulae & calculation explicitly!) (2.5 p)

- Use theoretical formula to calculate I_{disc} .

$$I_{disc} = \frac{MR^2}{2}$$

a) Moment of Inertia of the disk (Theoretical)

- Use period formula for torsion pendulum, calculate torsion constant.

$$T = 2\pi \sqrt{\frac{I}{\kappa}}$$

b) Torsion constant of the rod (Empirical)

$\kappa =$

- Use period formula and calculated torsion constant, determine $I_{total} = I_{disc} +$

$$T = 2\pi \sqrt{\frac{I_{total}}{\kappa}}$$

Find I_{total}

c) Total Moment of Inertia of the disk and the ring (Empirical-use your κ)

$I_{total} =$

I_{ring}

- Calculate I_{ring}

$$I_{ring} = I_{total} - I_{disc}$$

d) Moment of Inertia of the Ring (Empirical – use your I_{total} and I_{disc})

$I_{ring-EV} =$

1 8 6 3

ANGULAR HARMONIC MOTION

- Use theoretical formula and calculate I_{ring} .

$$I_{ring} = \frac{1}{2} M \left[(\bar{R}_{inner})^2 + (\bar{R}_{outer})^2 \right]$$

Compare empirical and theoretical values of I_{ring} .

e) Moment of Inertia of the Ring (Theoretical)

$I_{ring-TV} =$

Calculate the percentage error for Moment of Inertia of the Ring. Accuracy matters in this part: (1.1 p)

Error for $I_{ring} =$