

## Pre-Lab Report

Lab section:

Name & Surname:

Table #:

***Before the Lab complete this page YOURSELF! Hand it in in the first 5 min. of the session PERSONALLY!***

**You MUST justify your answers and show all steps. NO COPYCAT answers, or NO credits!**

**Please read the relevant presentation on PHYS LAB Website.**

**Q1.** If you apply Kirchoff's law to the circuit you will get the following relation:

$$L \frac{d^2q}{dt^2} + R \frac{dq}{dt} + \frac{q}{C} = V_{app}(t)$$

Convince yourself by inserting  $q(t) = q_0 A e^{-Rt/2L} \sin(\omega_0 t + \delta)$  with  $\omega_0 = \sqrt{\frac{1}{LC} - \frac{R^2}{4L^2}}$  is a solution to this equation. **Show your calculations below explicitly or no credits!**

(2<sup>nd</sup> Question is on the next page!)



## #1 Electromagnetic Oscillations in an RLC Circuit

**Q2. Show dimension analysis** for Inductance  $L$ , Capacitance  $C$  and Resistance  $R$  clearly. **Show your calculations below explicitly or no credits!**



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**Complete this report YOURSELF except DATA taking parts! Use a pencil for plots only and a pen for the rest! Show your work clearly, NO COPYCAT analysis allowed, or NO credits!**

**OBJECTIVE :** To study the oscillations of potential difference across a charged capacitor in series with a resistor and an inductor.

**THEORY :** In a series RLC circuit, the Kirchoff's loop rule results in the following:

$$L \frac{di}{dt} + Ri + \frac{q}{C} = V_{app}(t) \quad \text{or} \quad L \frac{d^2q}{dt^2} + R \frac{dq}{dt} + \frac{q}{C} = V_{app}(t)$$

since  $I = dq/dt$ . This is an equation for a damped oscillator driven by a time dependent voltage source or a signal generator. There are three different combinations of R, L, and C values where we can get specific solutions to this equation for a square wave signal as the applied voltage.

### **Underdamped:**

If the values satisfy the following conditions, the circuit will be underdamped:

$$\frac{R^2 C}{4L} < 1$$

Then the solution will be:

$$q(t) = q_o A e^{(-Rt/2L)} \sin(\omega_o t + \delta)$$

and the voltage across the capacitor will be:

$$V_C(t) = V_o B e^{(-Rt/2L)} \sin(\omega_o t + \delta),$$

where  $V_o$  is the voltage when the square wave is at the maximum value and  $\delta$  is the phase.  $\omega_o$  is given by:

$$\omega_o = \sqrt{\frac{1}{LC} - \frac{R^2}{4L^2}}$$

Oscillations decay exponentially with a time constant  $2L/R$ . Signals reach their half values in:

$$t_{1/2} = \frac{2L}{R} \ln 2$$

which we can call half-life of the signals.



## #1 Electromagnetic Oscillations in an RLC Circuit

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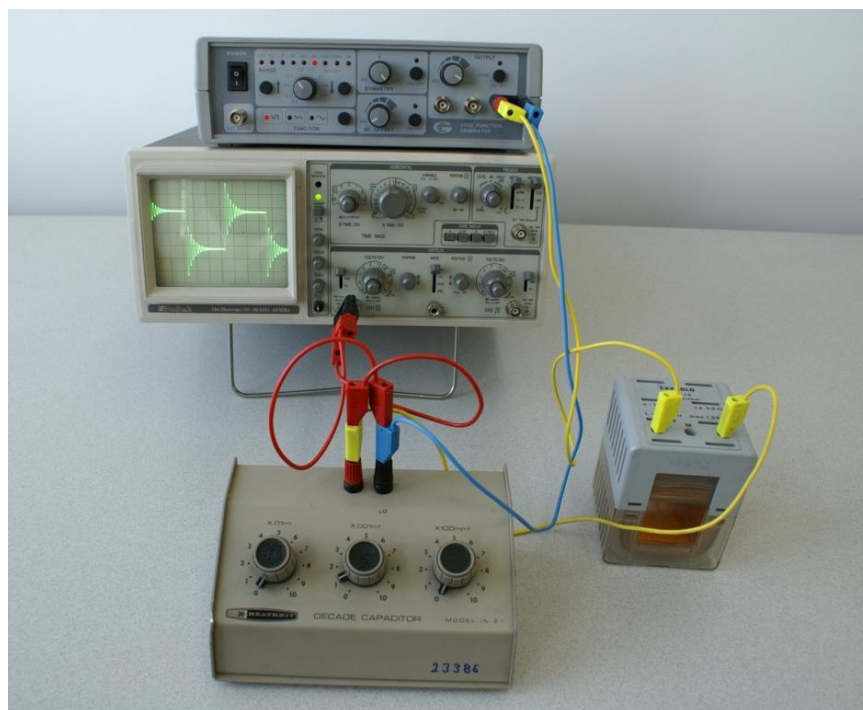
### *Critically Damped:*

If  $\frac{R^2 C}{4L} = 1$ , the circuit is critically damped. As you see from the equation for  $\omega_0$  above, the frequency of the oscillations is zero which means there is only an exponential decay.

### *Overdamped:*

If,  $\frac{R^2 C}{4L} > 1$  the circuit is overdamped. The frequency of the oscillations,  $\omega_0$ , is an imaginary number which means there is only an exponential decay similar to the Critically Damped Case.

**APPARATUS :** Capacitance and resistance boxes, inductor with an iron block, oscillator, oscilloscope.



### **PROCEDURE :**

- Connect the circuit by using the A-E terminals of the 1000 turn coil for the inductor and  $0.001\mu\text{F}$  capacitor, turn on the oscilloscope and make the initial adjustments. Internal resistance of the square wave generator and the coil resistance will be the total resistance in the circuit.
- Adjust the square wave frequency and the sweep frequency of the oscilloscope so that



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one complete cycle of decaying oscillations cover the whole screen of the oscilloscope. Record the value of the sweep frequency in your report.

- Choose two peaks at least 5-6 cm far from each other and count the number of the complete cycles in this chosen range  $l$ . Determine the length of one complete cycle, period, and the frequency of the decaying oscillations.
- Measure the half-life of the decaying oscillations.
- Using the half-life equation, calculate the inductance  $L$  of the coil in millihenries and calculate the frequency of oscillations by using this value.

$$t_{1/2} = \frac{2L}{R} \ln 2$$

$$f_o = \frac{1}{2\pi} \left[ \frac{1}{LC} - \frac{R^2}{4L^2} \right]^{1/2}$$

- When a piece of iron is inserted into a coil, a large change occurs in the inductance of the coil. With the iron fully inserted, determine the new value of the inductance.

### CIRCUIT DIAGRAM

Draw the circuit diagram



## DATA & CALCULATIONS

Description / Notation	Value & Unit	# of Significant Figures
Capacitance $C$	= .....	.....
Resistance $R$	= .....	.....
Frequency of the Square Wave Generator $f_{SWG}$	= .....	.....

Description / Notation	Value & Unit	# of Significant Figures
[TIME / DIV] Dial of the Oscilloscope <u>without</u> Iron Block	= .....	.....
[TIME / DIV] Dial of the Oscilloscope <u>with</u> Iron Block	= .....	.....
Length between the chosen peaks $\ell$	= .....	.....
Number of complete Cycles in $\ell$ $n$	= .....	.....



## DATA & CALCULATIONS

### WITHOUT IRON BLOCK INSIDE THE INDUCTOR

Description / Symbol		Value / Calculations	Result
		(show each step)	
Half-Life	$t_{1/2}(\text{cm}) =$	.....	.....
Half-Life	$t_{1/2}(\text{sec}) =$	.....	.....
Inductance			
of the coil	$L_1 =$	.....	.....
		.....	
Wavelength	$\lambda =$	.....	.....
Period of the			
Oscillations	$T =$	.....	.....
Frequency of the			
Oscillations	$f_{\text{measured}} =$	.....	.....
Frequency of the			
Oscillations	$f_{\text{calculated}} =$	.....	.....
<b>% Error for <math>f</math>:</b>			

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## WITH IRON BLOCK INSIDE THE INDUCTOR

Description / Symbol	Value / Calculations	Result
	(show each step)	
Half-Life	$t_{1/2}(\text{cm}) =$ .....	.....
Half-Life	$t_{1/2}(\text{sec}) =$ .....	.....
Inductance of the coil	$L_2 =$ .....	.....
	.....	

### QUESTION

What is the reason for the difference you observe when you insert the iron block inside the inductor?

Consult to the resources for this experiment from PHYS LAB Website:



PHY202 Intro



Presentation #1



PHY202 Lab Book

